

and for Fig. 9.3b, to the same approximation, it is evident that

$$I \approx E/R_e.$$

These two circuits are equivalent at resonance provided we set

$$R_e = L/Cr = Q\omega_o L = Q/\omega_o C = Q\sqrt{L/C} \quad (20)$$

Note that  $Q = R_e\sqrt{C/L}$ , and that  $R_e$  is the parallel resistance (across  $C$ ) equivalent to the series coil resistance  $r$ .

It has been shown that the circuit Fig. 9.3a with a condenser  $C$  having no losses and an inductance  $L$  having series coil resistance  $r$  may be replaced by the equivalent circuit Fig. 9.3b having an ideal tuned circuit  $LC$ , without losses, shunted by the resistor  $R_e$  having a value given by equation (20). It is obvious that the impedance of the parallel combination  $LCR_e$  in Fig. 9.3b at resonance is  $R_e$ , this being the "resonant impedance" of the circuit. At frequencies other than the resonant frequency, the impedance will be less than the "resonant impedance."

The values of  $Q$  in terms of series coil resistance  $r$  and equivalent parallel resistance  $R_e$  are grouped below for convenience.

$$\text{In terms of } r: \quad Q = \frac{\omega_o L}{r} = \frac{1}{\omega_o Cr} = \frac{1}{r} \sqrt{\frac{L}{C}}$$

$$\text{In terms of } R_e: \quad Q = \frac{R_e}{\omega_o L} = \omega_o CR_e = R_e \sqrt{\frac{C}{L}}$$

We can now consider the important practical case of the circuit shown in Fig. 9.4, in which a resistance  $R$  appears in shunt with the condenser  $C$ .  $R$  represents the effect of all insulation losses in condenser, coil, wiring, switches and valves, together with the plate or input resistance of the valves.

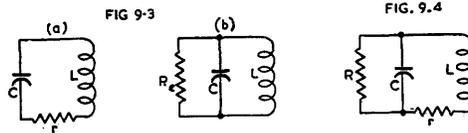


Fig. 9.3(a). Parallel resonance with series loss resistance.

Fig. 9.3(b). Parallel resonance with parallel loss resistance.

Fig. 9.4. Parallel resonance with both series and parallel loss resistances.

In the present case we have  $R$  in parallel with our equivalent parallel coil resistance  $R_e$  of Fig. 9.3b. The resultant parallel resistance at resonance, which we will call the **resonant impedance** is, of course,

$$R_D = \frac{1}{1/R + Cr/L} \quad (21)$$

Therefore, the **resultant value of  $Q$**  is

$$Q = \sqrt{\frac{C}{L}} \cdot R_D = \frac{1}{(1/R)\sqrt{L/C} + r\sqrt{C/L}} = \frac{1}{(\omega_o L/R) + (r/\omega_o L)} \quad (22)$$

Note that at the resonant frequency the expression  $\sqrt{L/C}$  is equal to the reactance of the inductance and also that of the condenser, i.e.

$$\omega_o L = \sqrt{L/C} = 1/\omega_o C. \quad (23)$$

See also Sect. 11 Summary of Formulae.