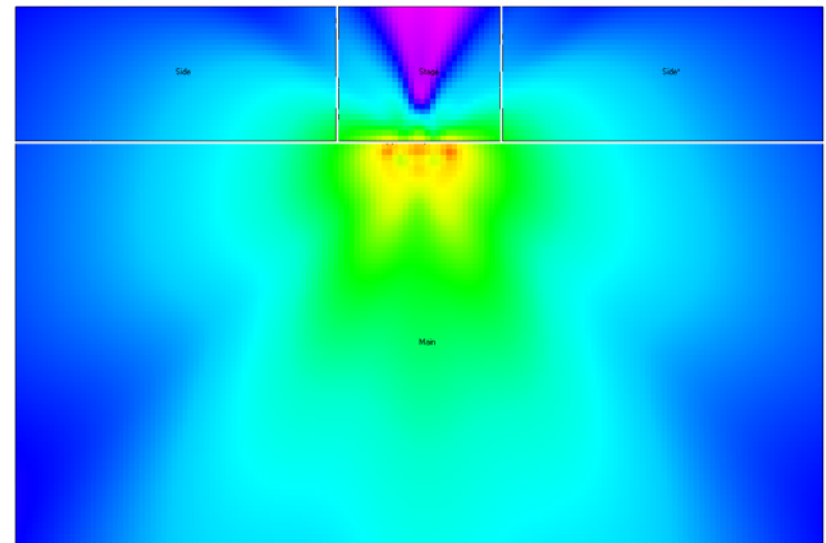
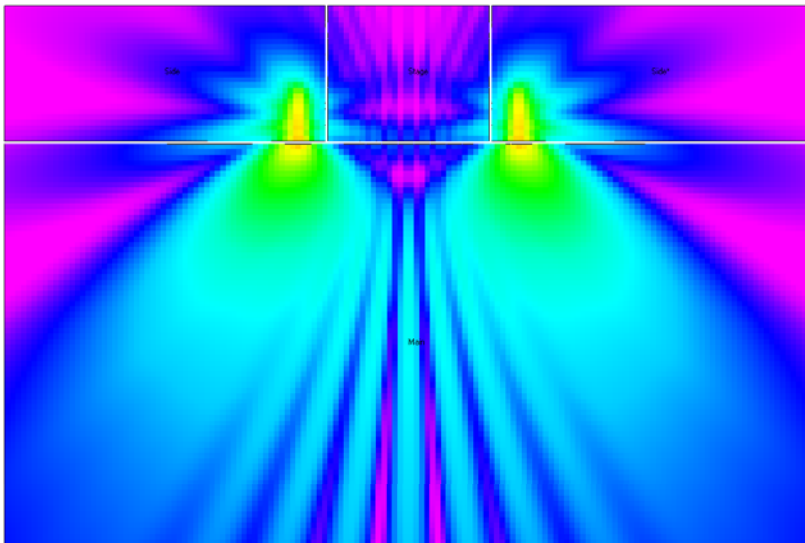
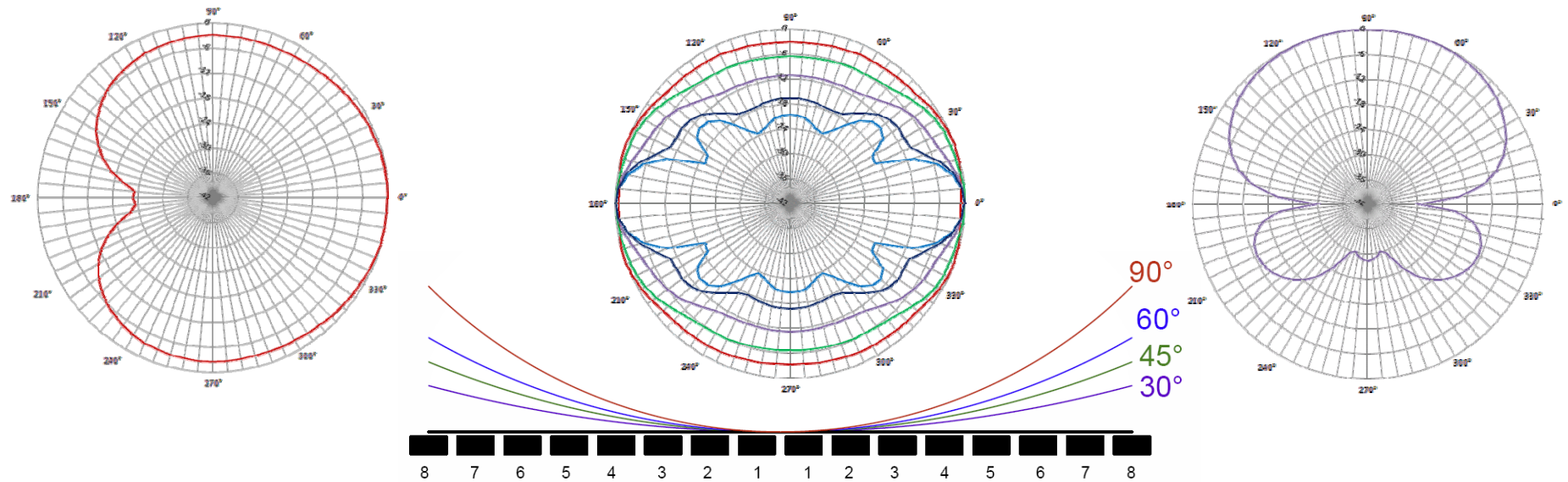
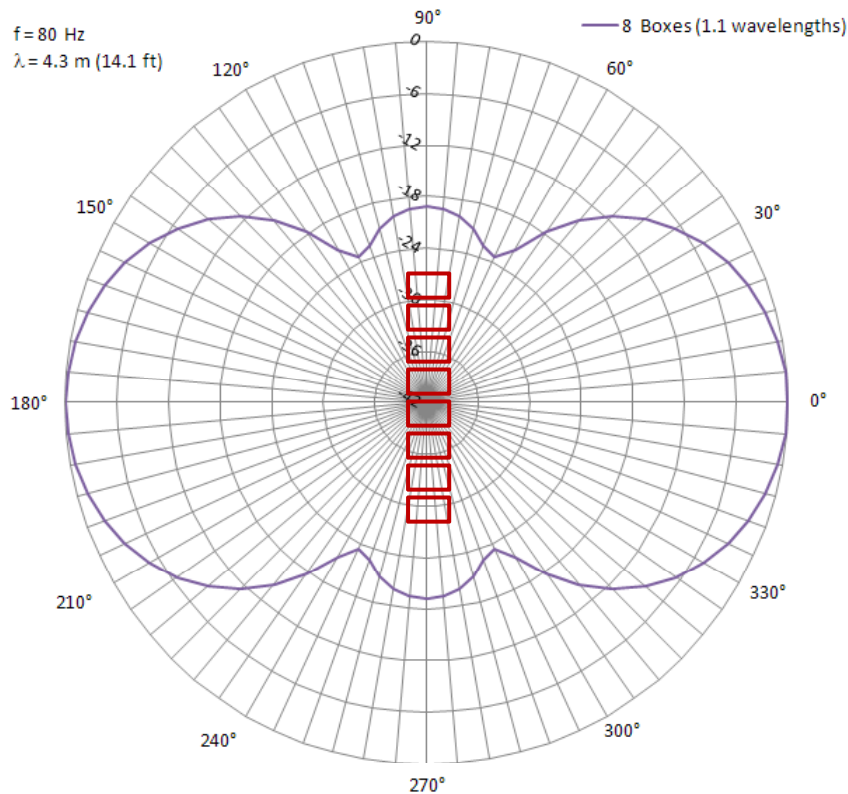




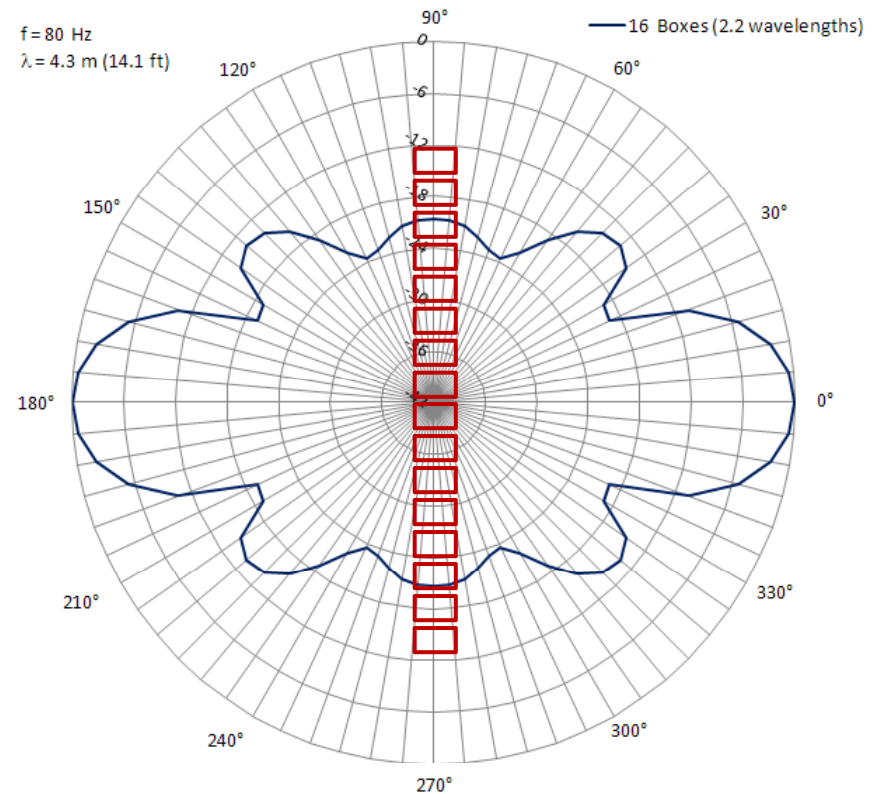
Subwoofer Arrays & Applications



Directivity is a Result of Source Size



80 Hz polar graph of 8x dual 18" subwoofers

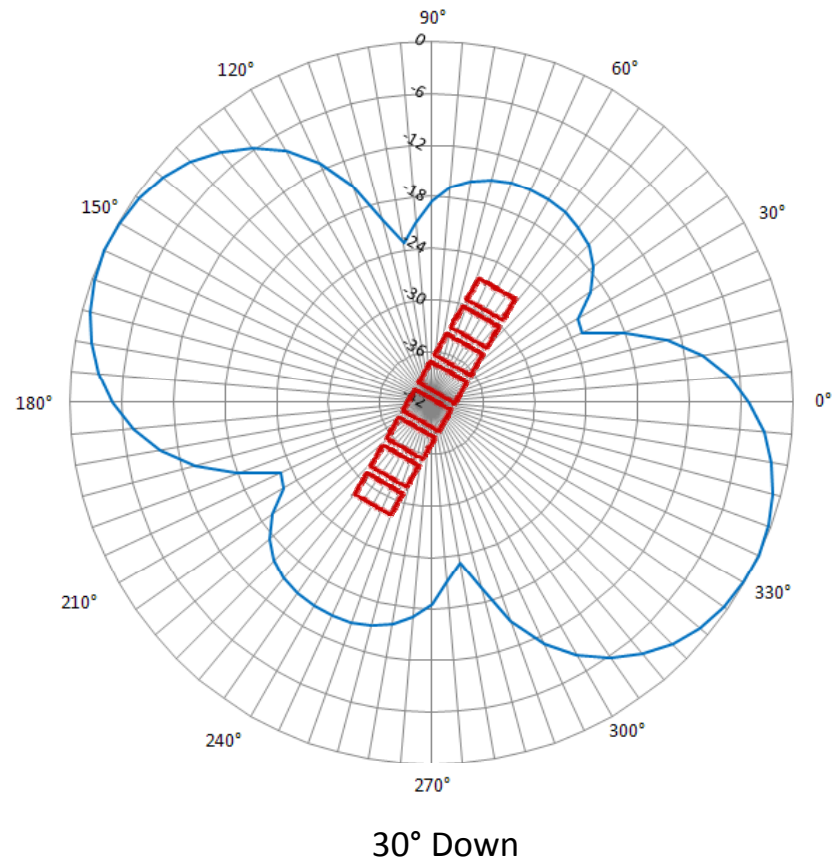
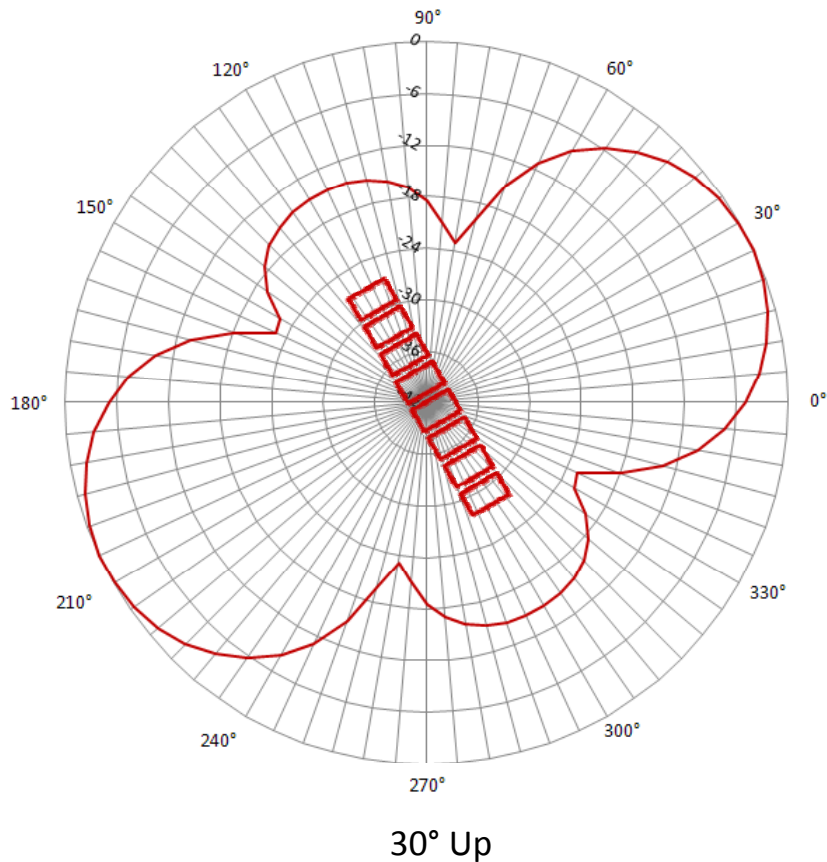


80 Hz polar graph of 16x dual 18" subwoofers

When the array size is one wavelength or greater there is substantial directivity control.

Steering the Main Lobe

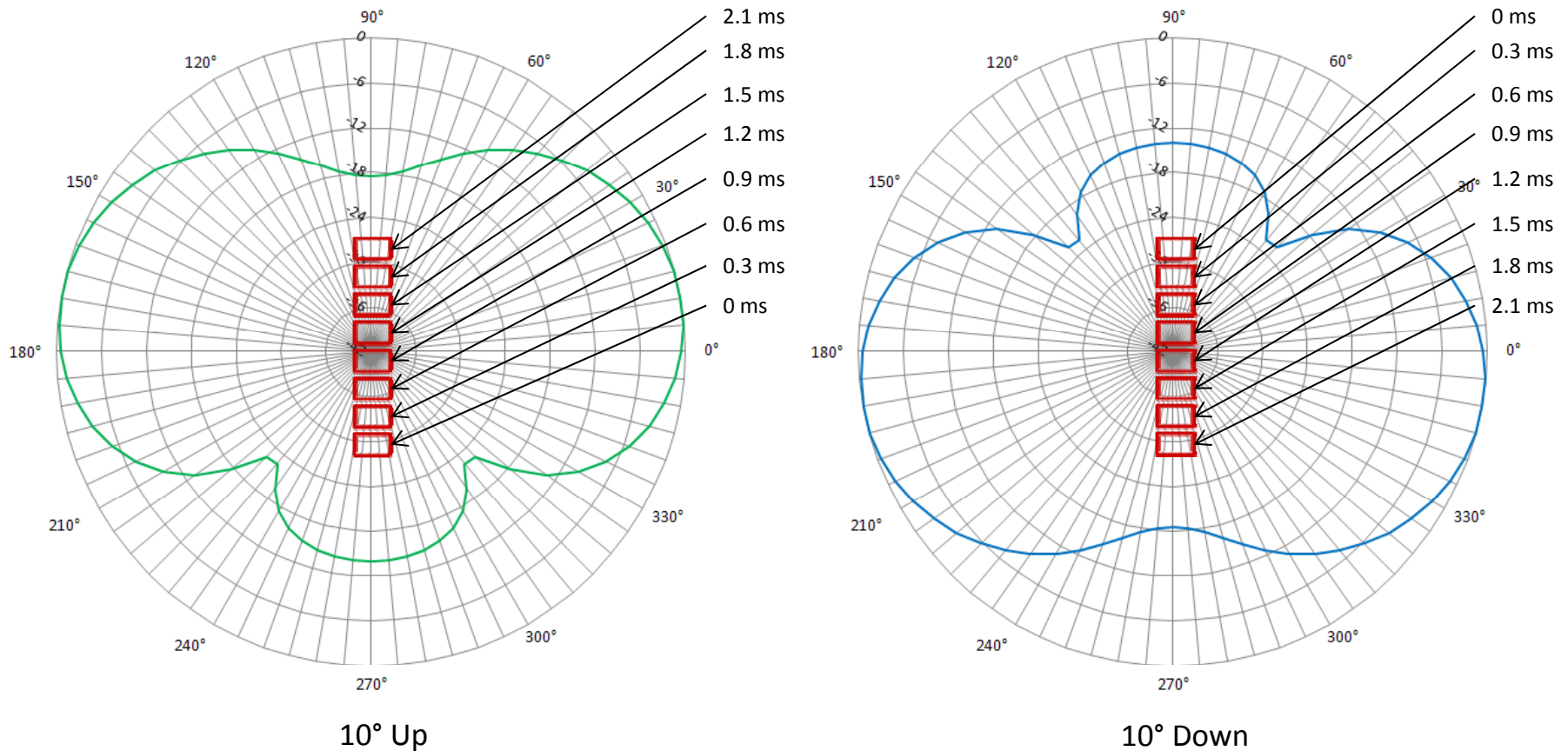
Mechanical Steering – the array is tilted



Note that the rear lobe also follows the orientation of the array. It points in the opposite direction of the front lobe.

Steering the Main Lobe

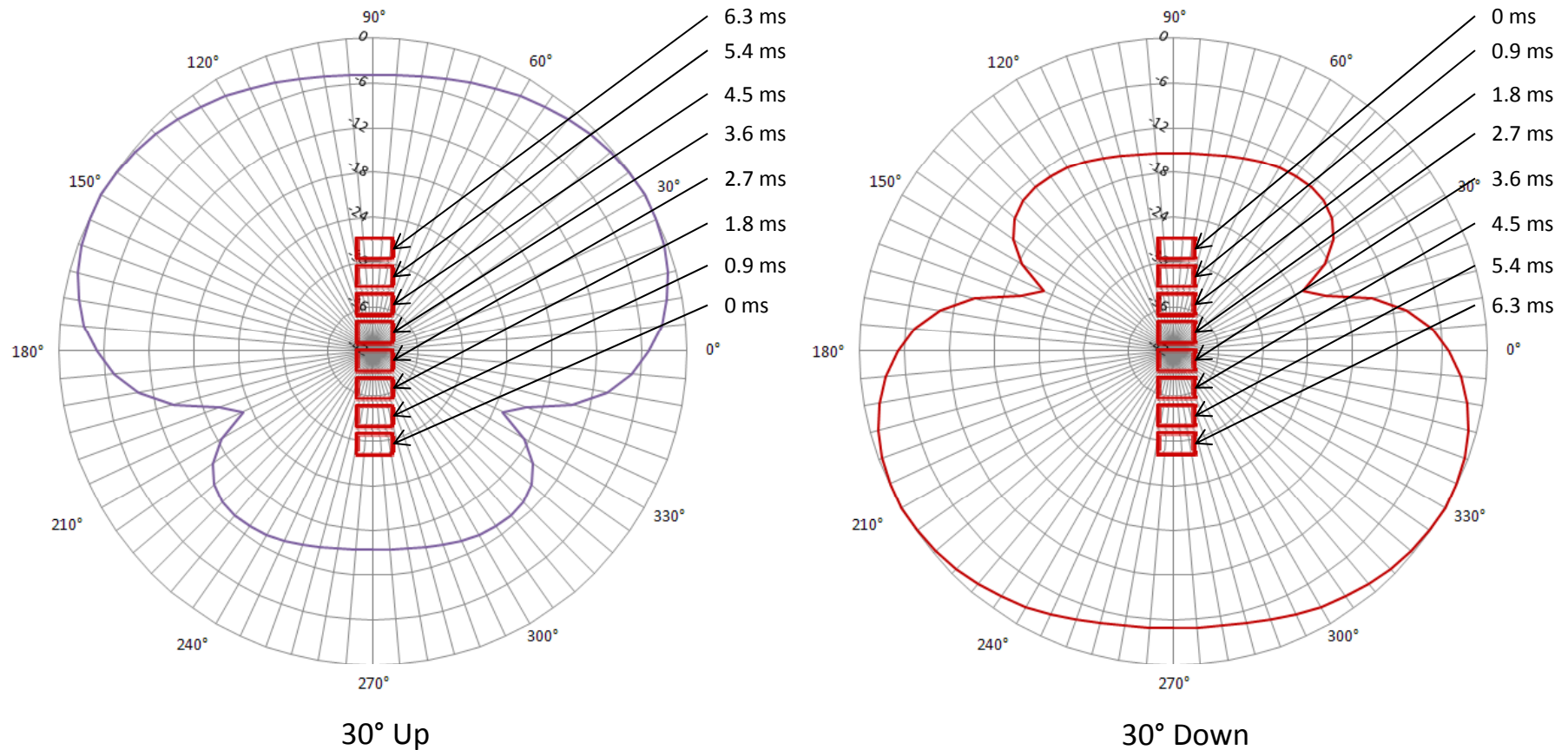
Electrical Steering – the same incremental delay is applied to each box



Note that the rear lobe is pointing in the **same** direction as the front lobe.

Steering the Main Lobe

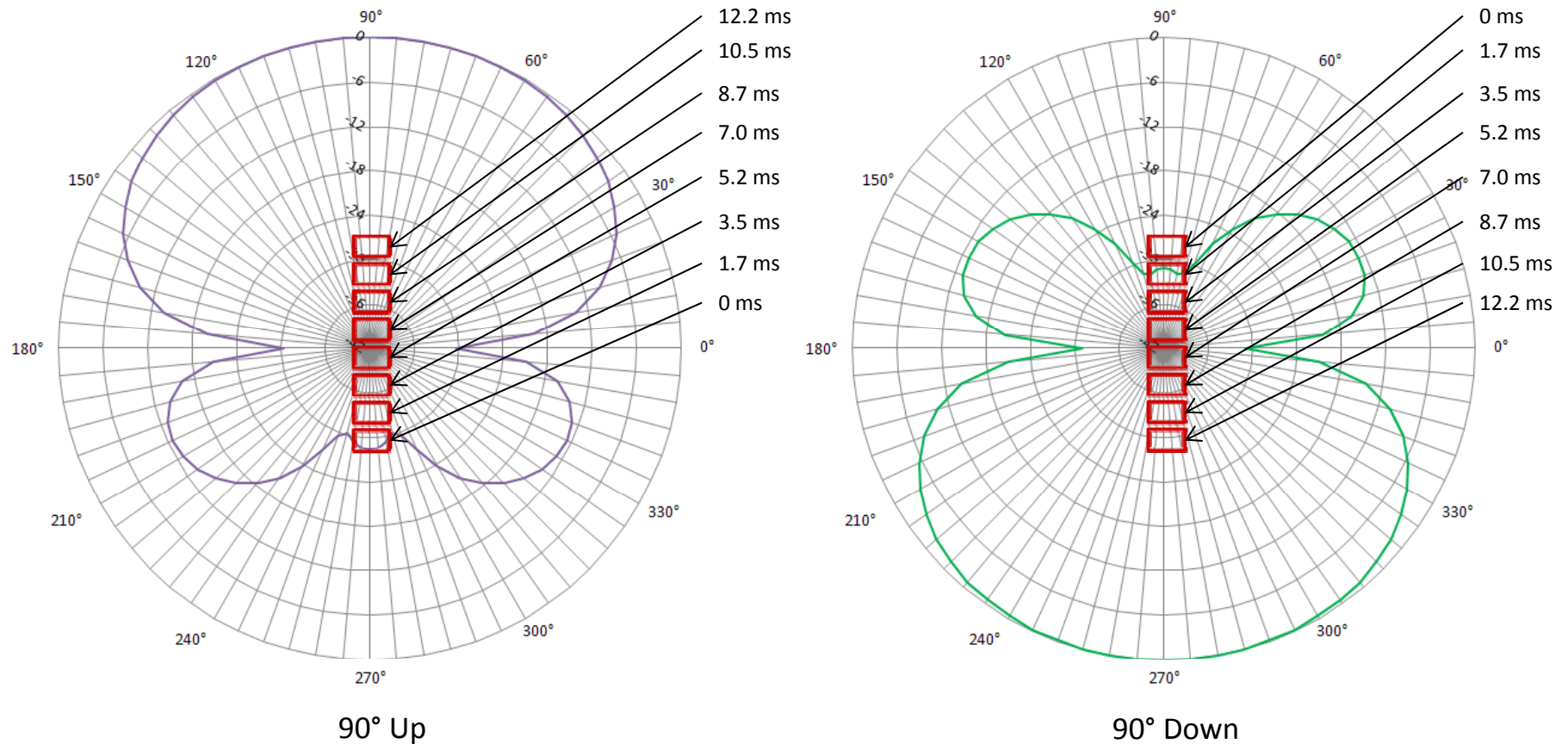
Electrical Steering – the same incremental delay is applied to each box



Note that as the steering increases the front and rear lobes begin to merge.

Steering the Main Lobe

End-Fire Array – when the inter-box delay is equal to the inter-box spacing



Each individual box is delayed back to the rear box so that, on-axis, all of the energy arrives at the same time.

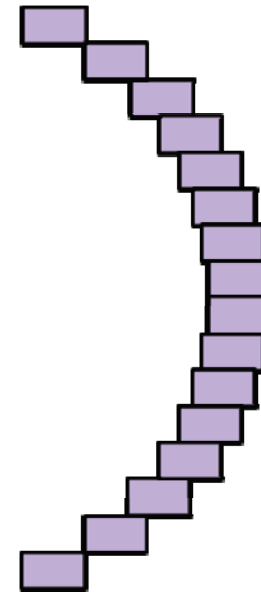
Wave Front Shaping – Broadening the Main Lobe

Curving the array will decrease the directivity and broaden the coverage pattern.

Often there may not be sufficient space for a curved subwoofer array or time to accurately position each box in the array.



16 Box Straight Array



16 Box Circular Curved Array

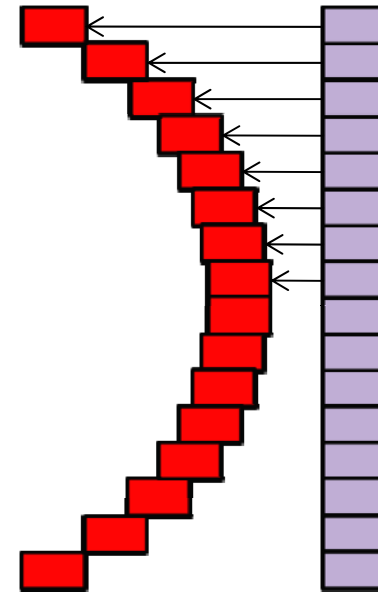
Wave Front Shaping – Broadening the Main Lobe

The array can be curved electrically, instead of mechanically, by using delay.

The boxes farther from the center must be delayed progressively more. The curve is symmetrical so one delay output can drive two boxes.



16 Box Straight Array



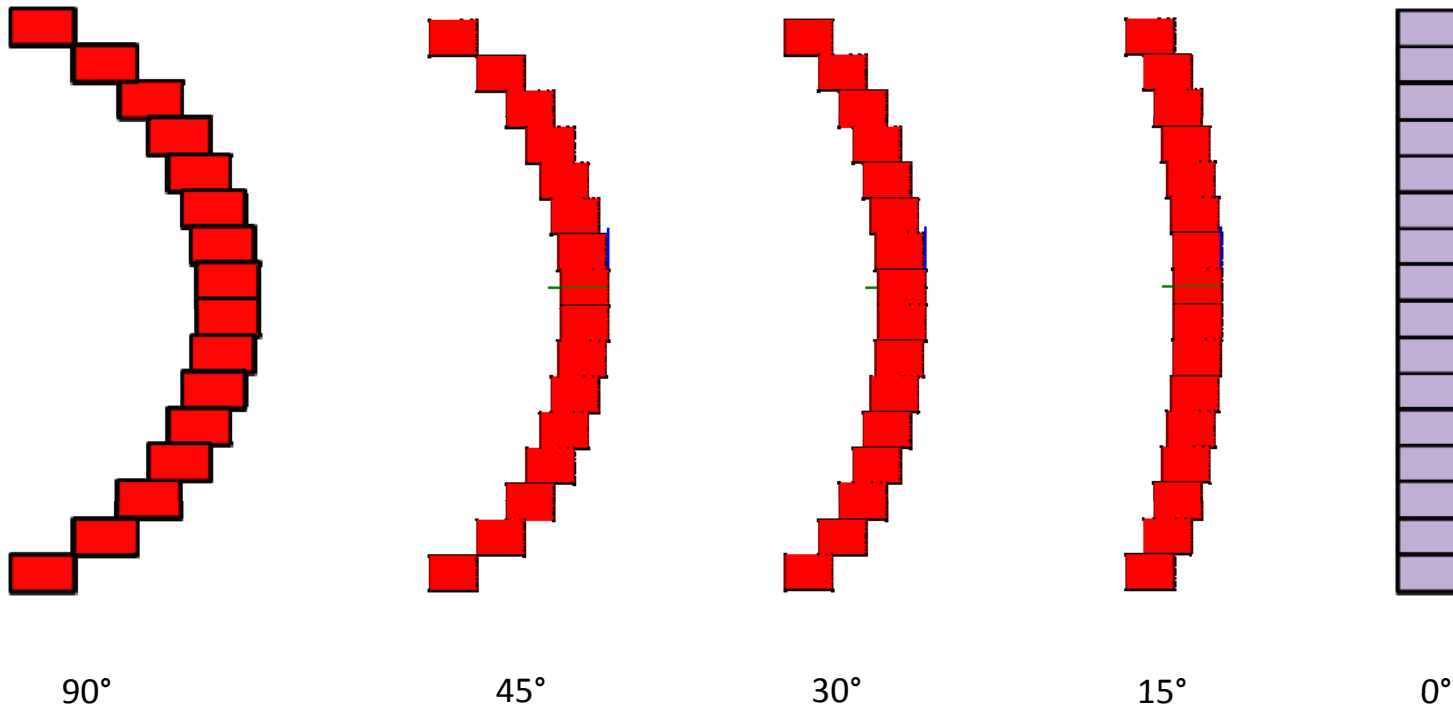
16 Box Circular Curved Array



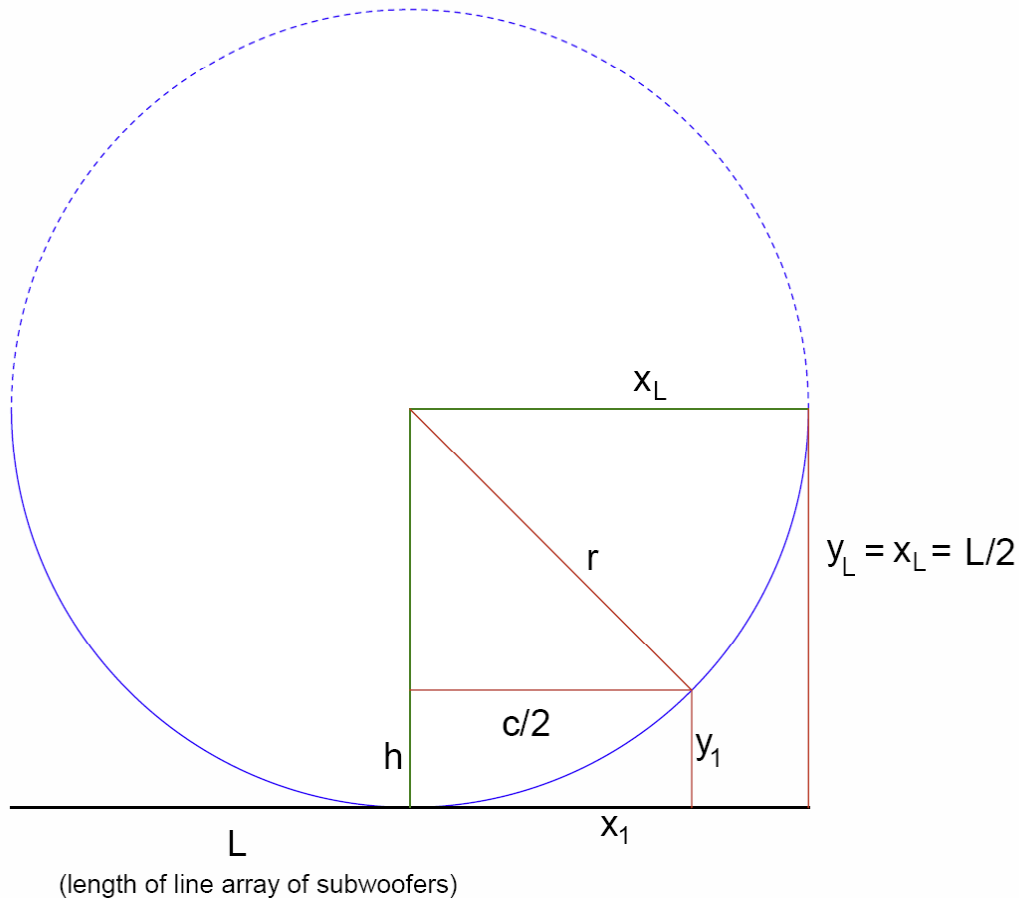
Wave Front Shaping – Broadening the Main Lobe

The array is configured mechanically as a straight line.

The amount of delay can be varied to yield any amount of curvature from 0° to 180°.



Wave Front Shaping – Broadening the Main Lobe



$$h = r - \frac{1}{2}(4r^2 - c^2)^{\frac{1}{2}}$$

$$y_1 = h$$

$$c/2 = x_1, \quad c = 2x_1$$

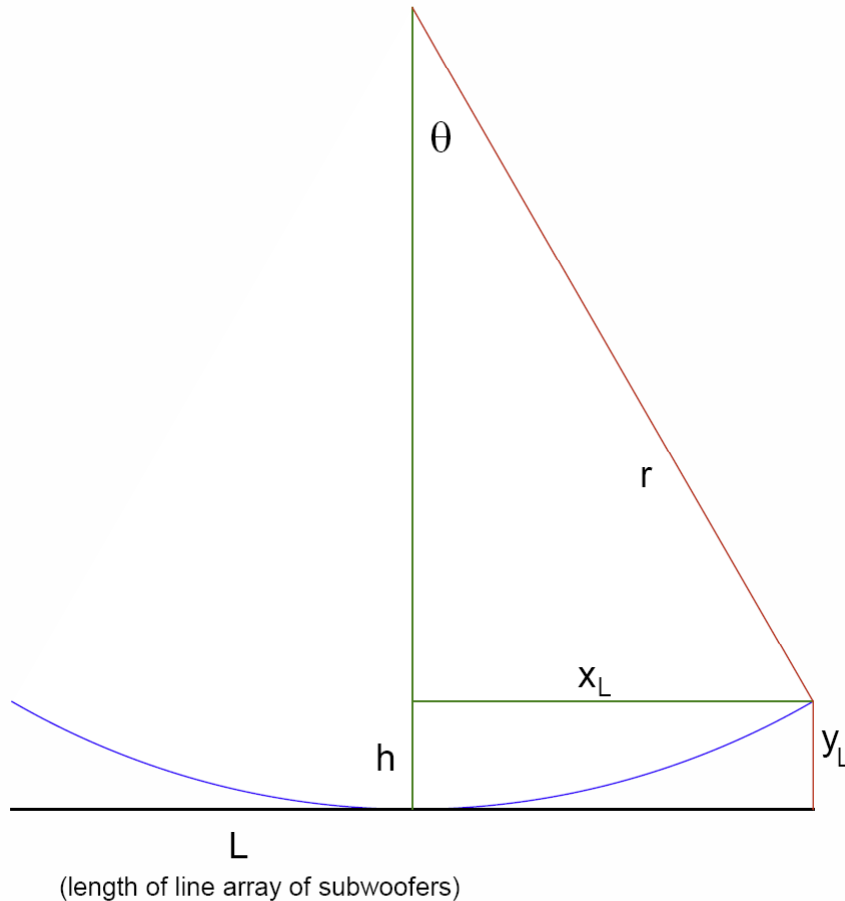
$$h = r - \frac{1}{2}(4r^2 - 4x_1^2)^{\frac{1}{2}}$$

$$h = r - (r^2 - x_1^2)^{\frac{1}{2}}$$

$$y_1 = r - (r^2 - x_1^2)^{\frac{1}{2}}$$

Line curved fully to 180° arc. Maximum curvature allowed.

Wave Front Shaping – Broadening the Main Lobe



For a smaller angle of curvature the radius has a larger value.

$$r = x_L / \sin(\theta)$$

$$(0^\circ \leq \theta \leq 90^\circ)$$

$$y_n = r - (r^2 - x_n^2)^{1/2}$$

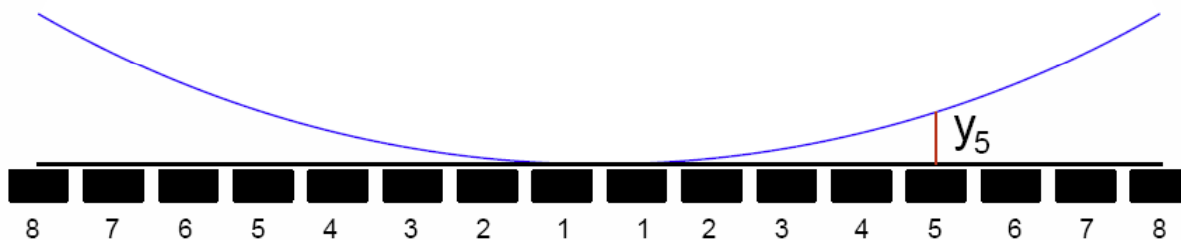
Line only partially curved to an angle of 2θ .



Wave Front Shaping – Broadening the Main Lobe

Delay times required for 60° curvature

Sub Spacing	1.050	Freq (spacing = $\lambda/4$)	81.90	Freq (spacing = $\lambda/2$)	163.81				
Number of Subs	16	Line Length	16.80	Freq (length = λ)	20.48				
Speed of Sound	344	Half Line Length	8.4						
Coverage Angle	60								
Desired Line Curvature (deg)	30.0								
radius	16.800	Source	Position (m)	Distance Offset	Normalized Offset	Delay for Curvature	Cabinet	Position	60° Delay
		1	0.525	0.01	0.00	0.000	Left 8	7.875	5.674
		2	1.575	0.07	0.07	0.191	Left 7	6.825	4.188
		3	2.625	0.21	0.20	0.576	Left 6	5.775	2.952
		4	3.675	0.41	0.40	1.159	Left 5	4.725	1.947
		5	4.725	0.68	0.67	1.947	Left 4	3.675	1.159
		6	5.775	1.02	1.02	2.952	Left 3	2.625	0.576
		7	6.825	1.45	1.44	4.188	Left 2	1.575	0.191
		8	7.875	1.96	1.95	5.674	Left 1	0.525	0.000
							Right 1	-0.525	0.000
							Right 2	-1.575	0.191
							Right 3	-2.625	0.576
							Right 4	-3.675	1.159
							Right 5	-4.725	1.947
							Right 6	-5.775	2.952
							Right 7	-6.825	4.188
							Right 8	-7.875	5.674

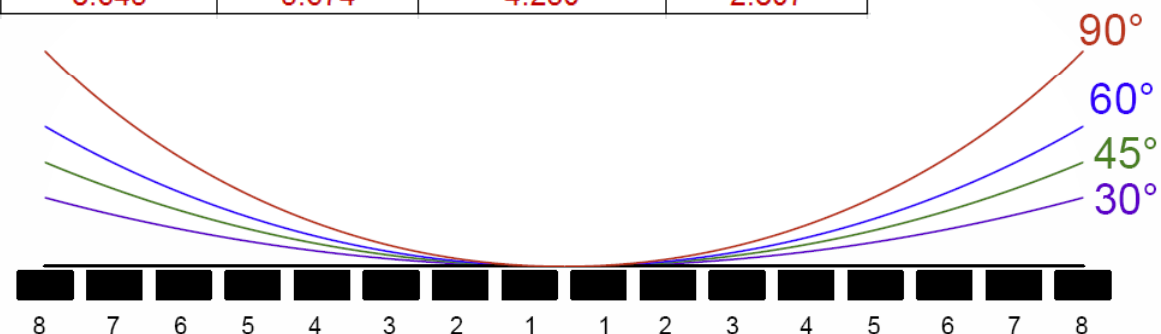




Wave Front Shaping – Broadening the Main Lobe

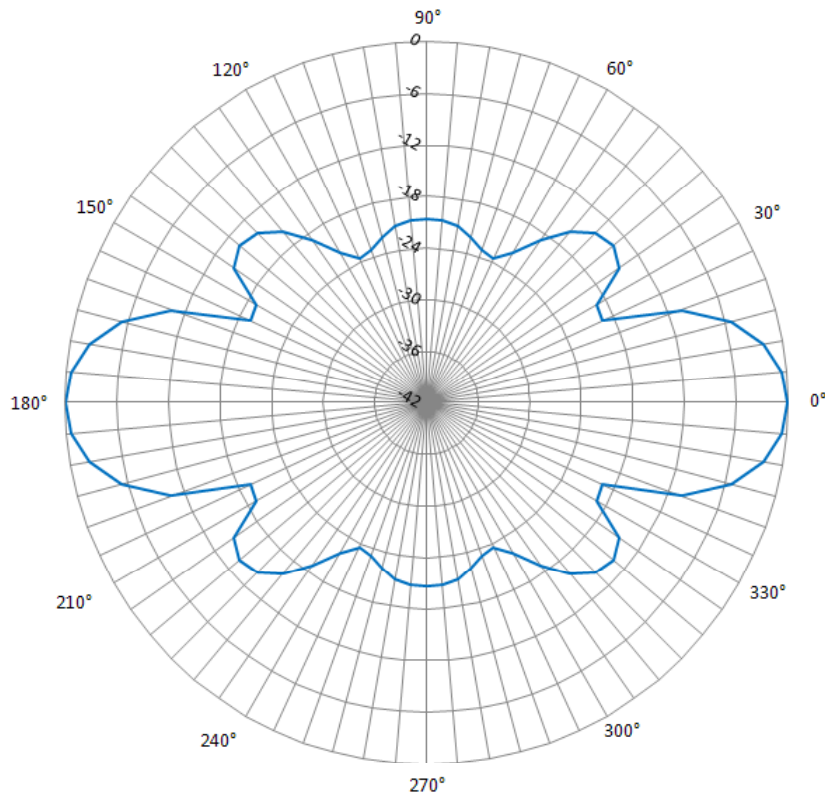
Delay times required for various curvatures

Cabinet	Position	90° Delay	60° Delay	45° Delay	30° Delay
Left 8	7.875	8.645	5.674	4.230	2.807
Left 7	6.825	6.234	4.188	3.145	2.097
Left 6	5.775	4.321	2.952	2.230	1.493
Left 5	4.725	2.815	1.947	1.478	0.993
Left 4	3.675	1.660	1.159	0.882	0.594
Left 3	2.625	0.820	0.576	0.440	0.297
Left 2	1.575	0.271	0.191	0.146	0.099
Left 1	0.525	0.000	0.000	0.000	0.000
Right 1	-0.525	0.000	0.000	0.000	0.000
Right 2	-1.575	0.271	0.191	0.146	0.099
Right 3	-2.625	0.820	0.576	0.440	0.297
Right 4	-3.675	1.660	1.159	0.882	0.594
Right 5	-4.725	2.815	1.947	1.478	0.993
Right 6	-5.775	4.321	2.952	2.230	1.493
Right 7	-6.825	6.234	4.188	3.145	2.097
Right 8	-7.875	8.645	5.674	4.230	2.807

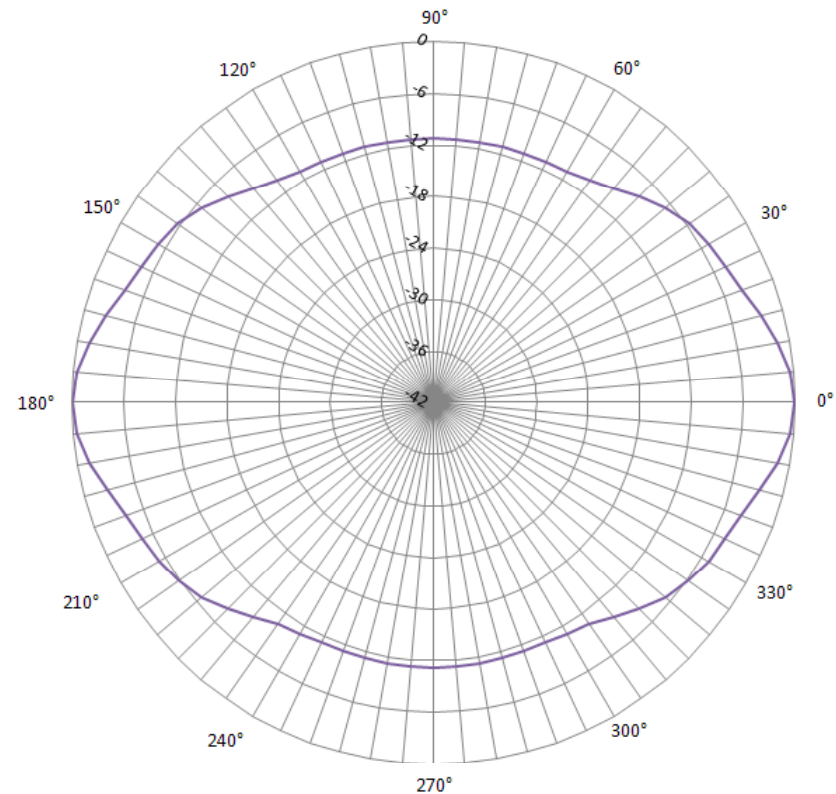


Wave Front Shaping – Broadening the Main Lobe

Comparison of straight array with various amounts of curvature via delay



16 Box Straight Array, No Delay Curvature

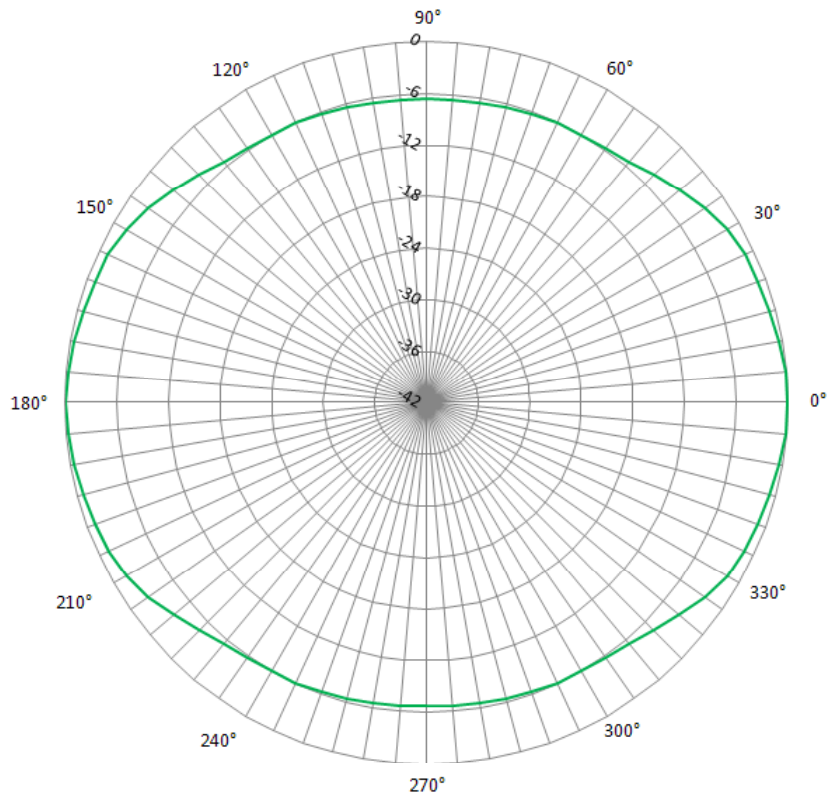


16 Box Straight Array, Curved 30° with Delay

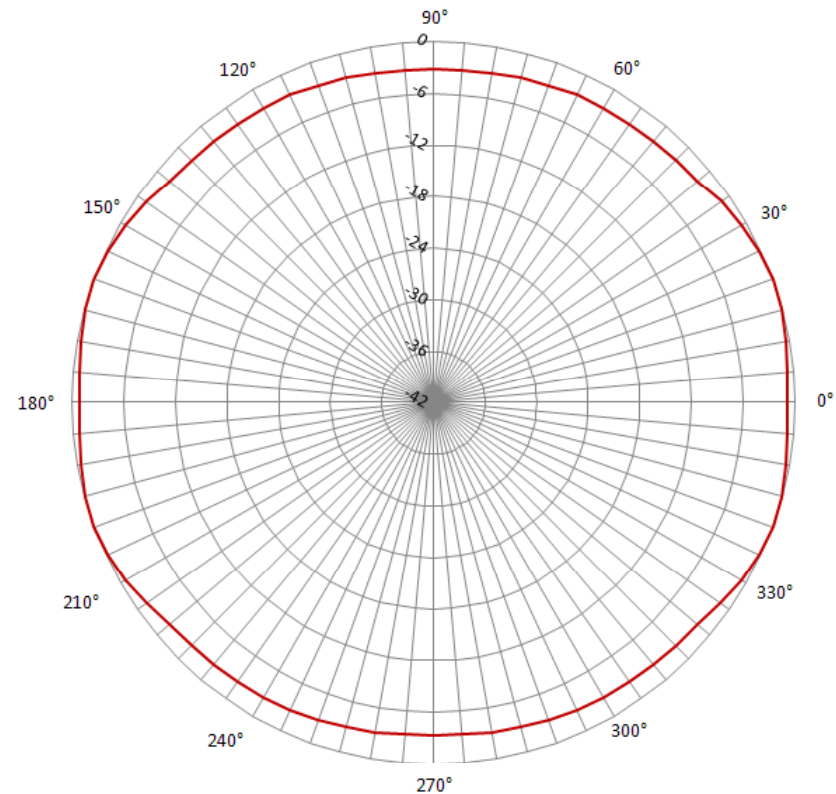


Wave Front Shaping – Broadening the Main Lobe

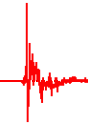
Comparison of straight array with various amounts of curvature via delay



16 Box Straight Array, Curved 45° with Delay

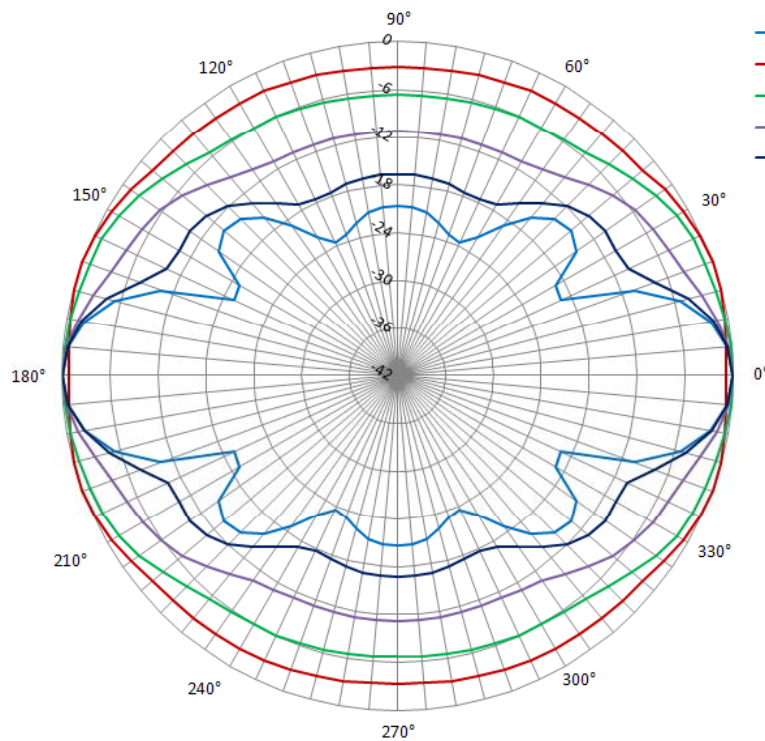


16 Box Straight Array, Curved 90° with Delay



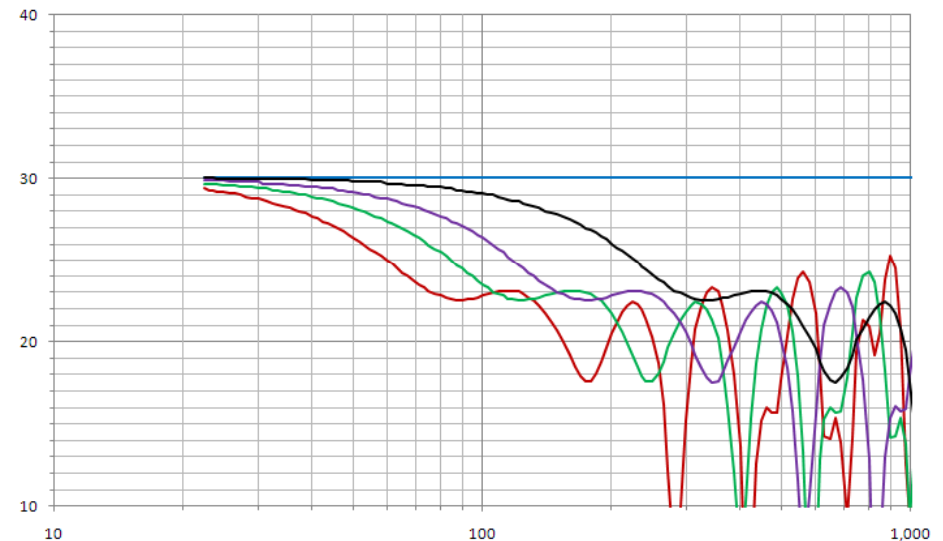
Wave Front Shaping – Broadening the Main Lobe

Comparison of straight array with various amounts of curvature via delay



Polar Response at 80 Hz

- 16 Straight
- 16 Straight, Delay 90°
- 16 Straight, Delay 45°
- 16 Straight, Delay 30°
- 16 Straight, Delay 15°



On-Axis Magnitude Response

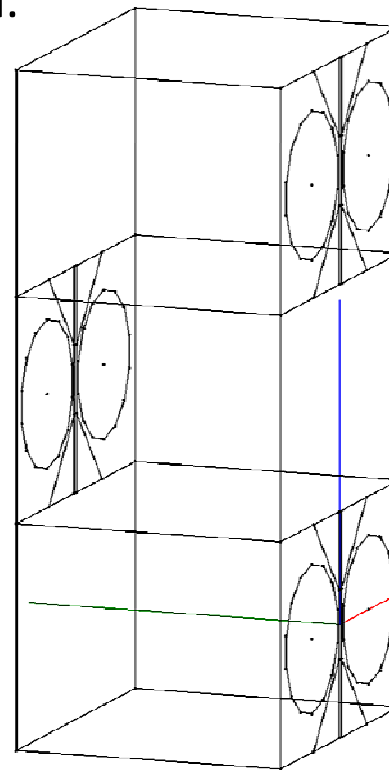
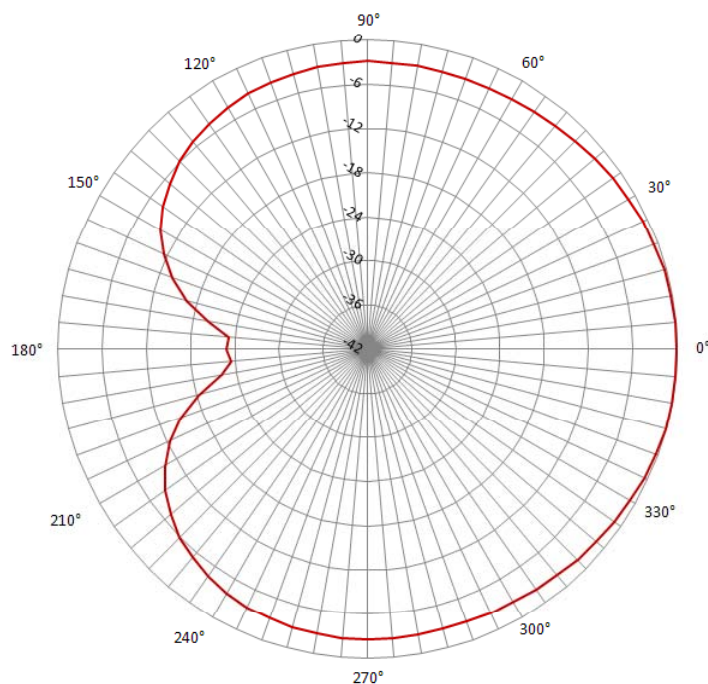
16 Box Straight Array, Curved with Delay

Cardioid Array – Controlling Rear Radiation

Sources must be physically offset by $\frac{1}{4}$ wavelength at the highest frequency to be used.

Rear source must be delayed by $\frac{1}{4}$ wavelength at the highest frequency to be used.

Polarity of rear source must be inverted.

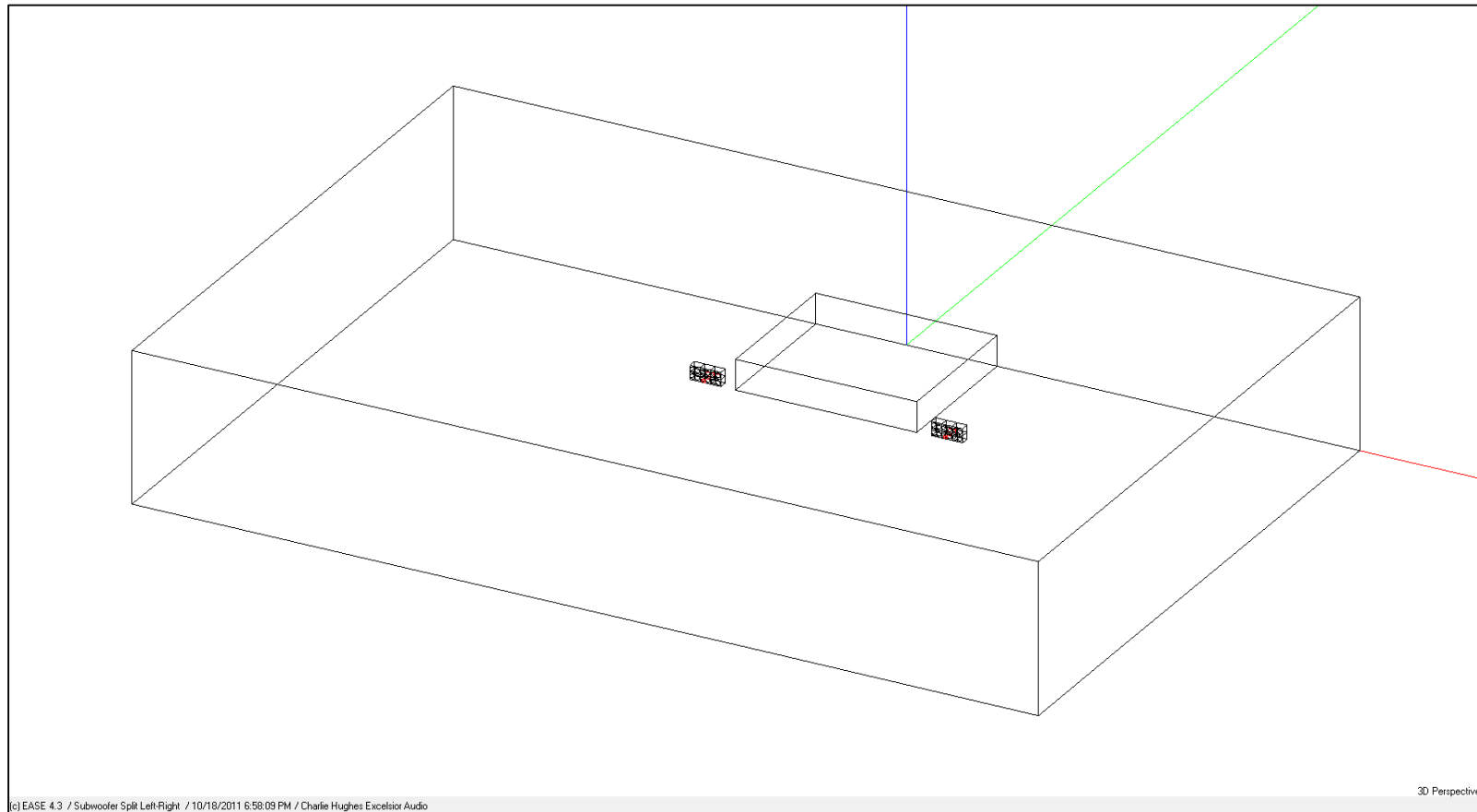


3 Box Cardioid Array

Vertical symmetry keeps vertical pattern symmetrical.

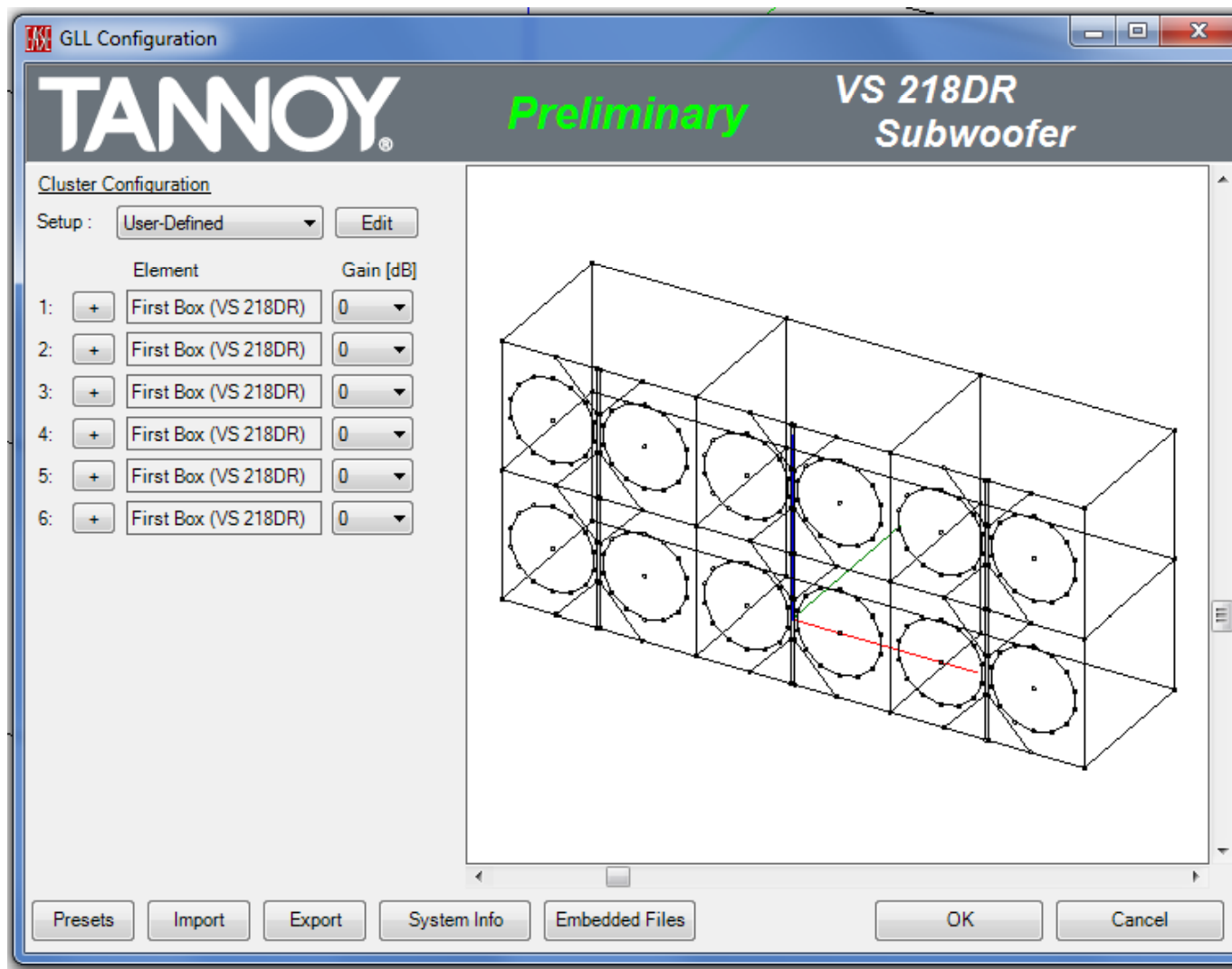
Conventional Stacks Split Left & Right

Large room (walls, floor, & ceiling are non-reflective; direct field only)
Stage approx. 60 ft (18.3 m) wide. Subs spaced approx. 80 ft (24.4 m).

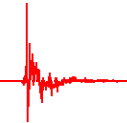


Conventional 2 x 3 stack on left & right side of the stage

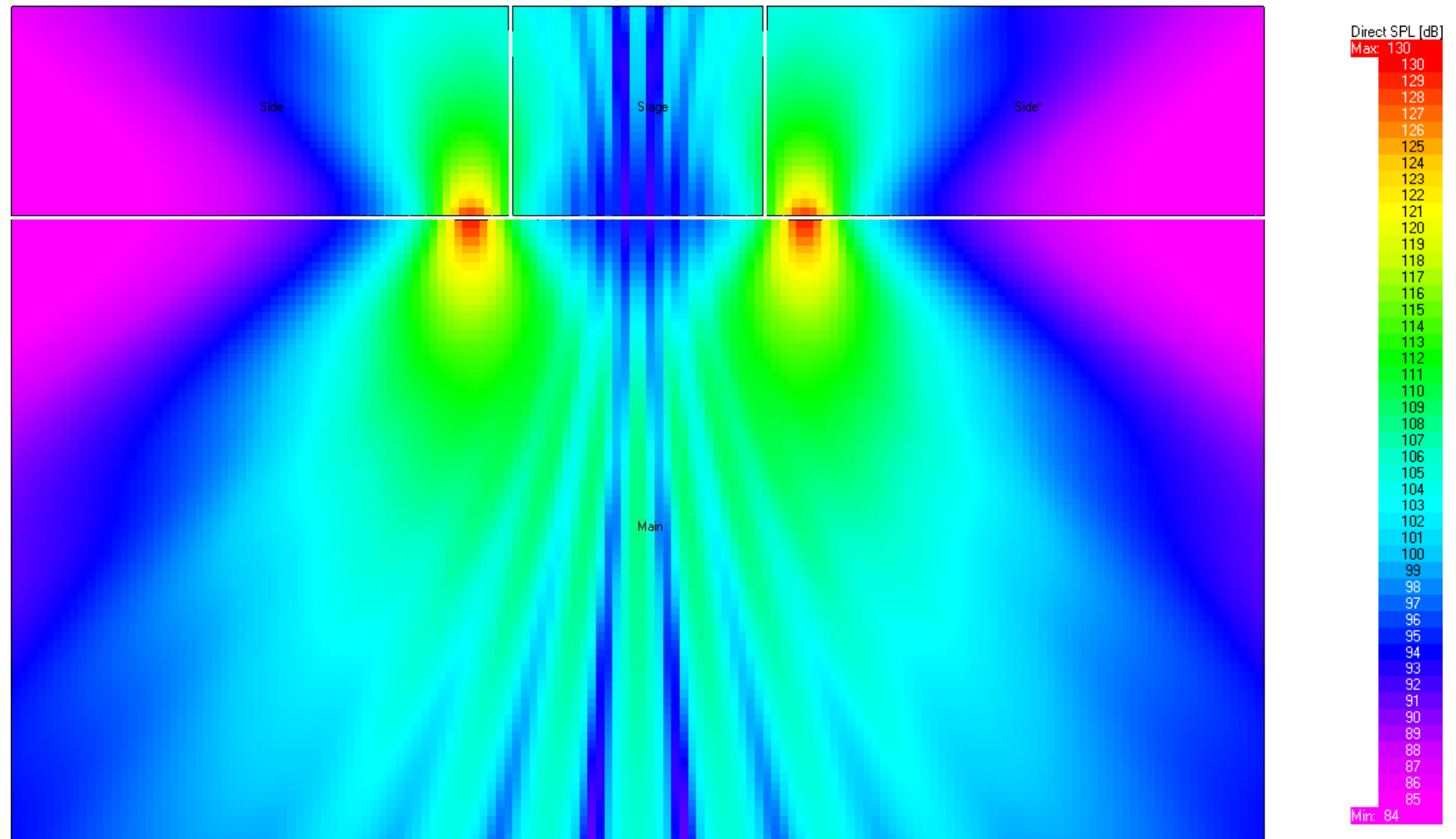
Conventional Stacks Split Left & Right



Conventional 2 x 3 stack on left & right side of the stage



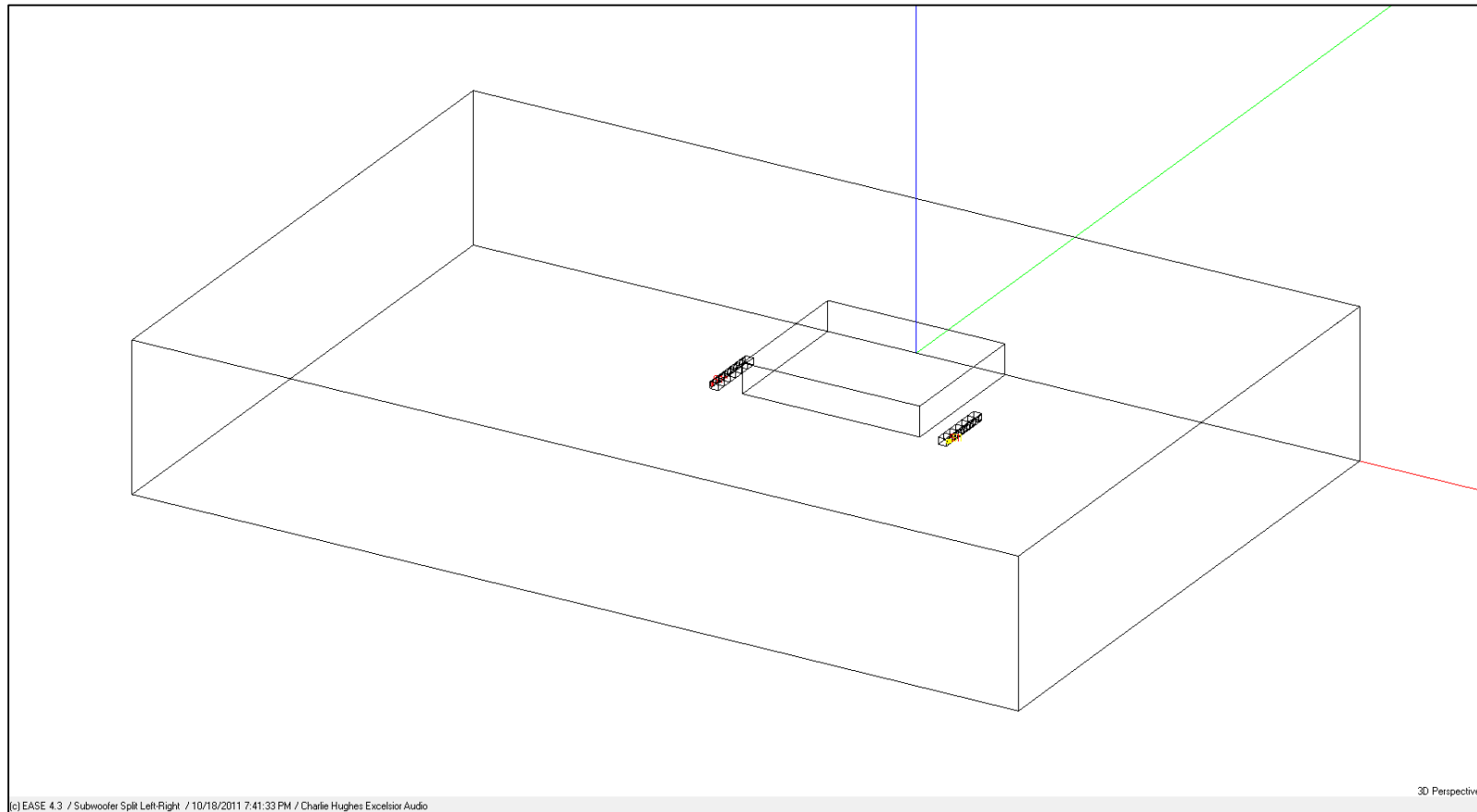
Conventional Stacks Split Left & Right



SPL Map

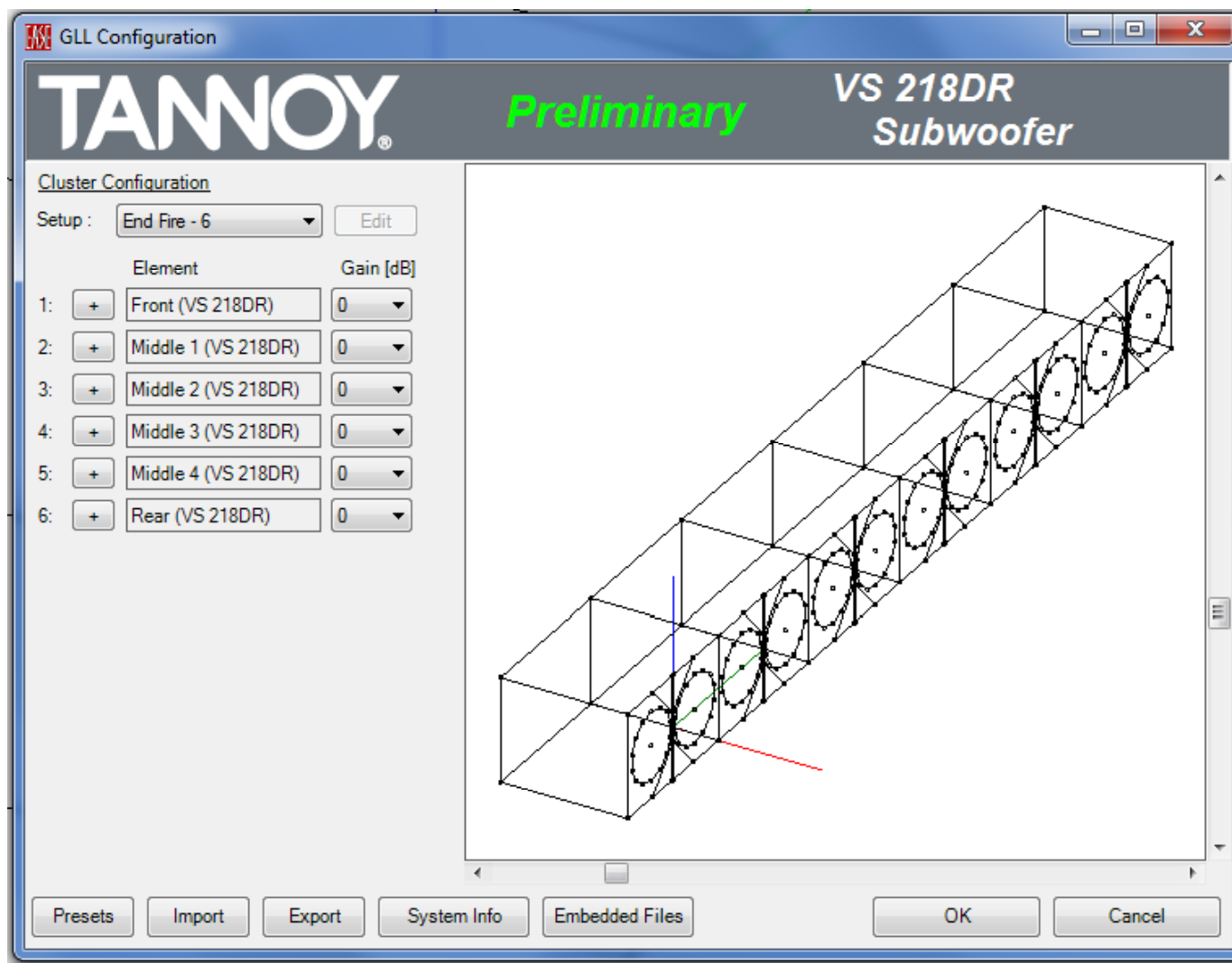
End-Fire Arrays Split Left & Right

Large room (walls, floor, & ceiling are non-reflective; direct field only)
Stage approx. 60 ft (18.3 m) wide. Subs spaced approx. 80 ft (24.4 m).

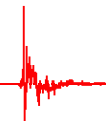


6 box end-fire array on left & right side of the stage

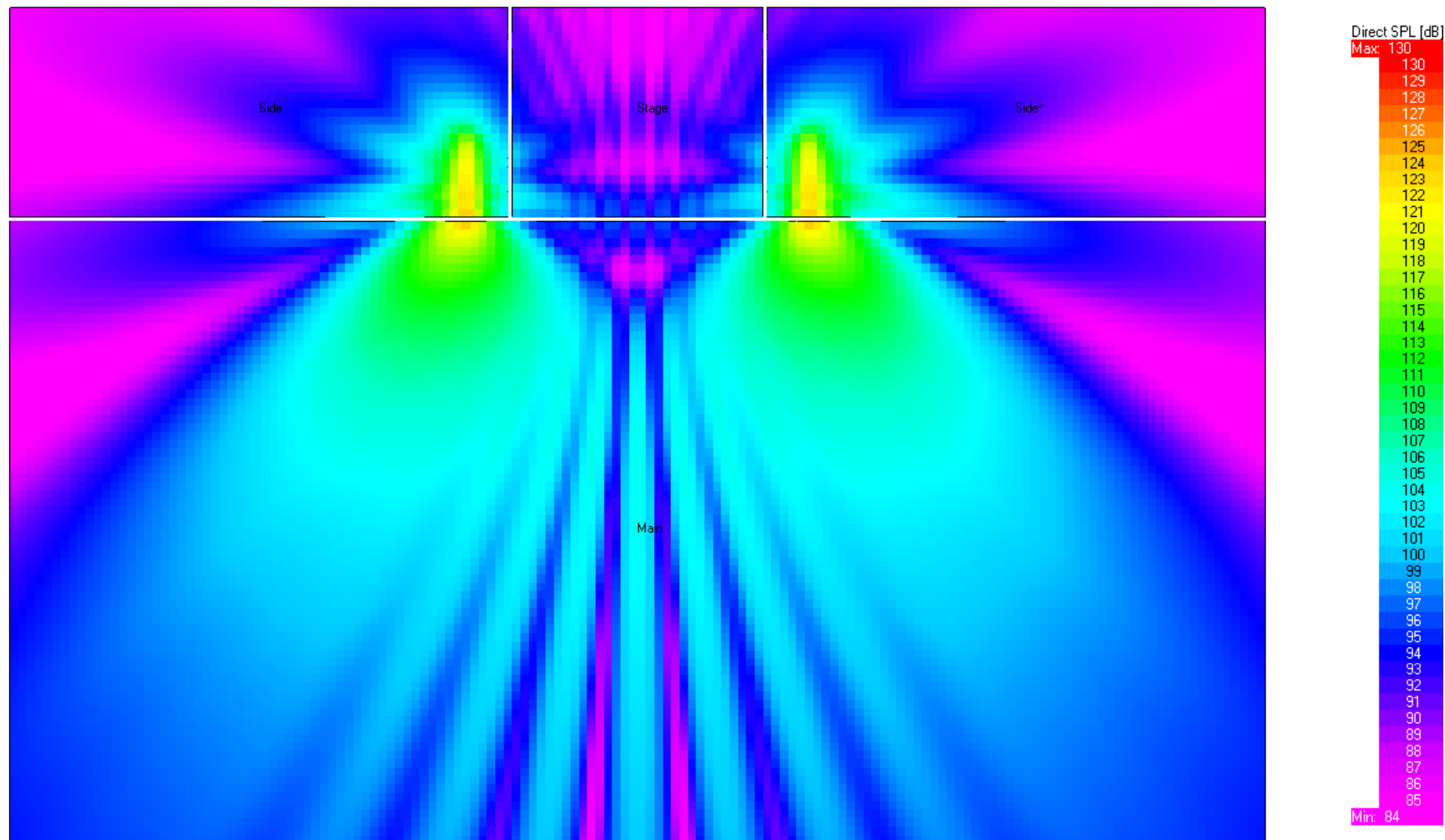
End-Fire Arrays Split Left & Right



6 box end-fire array on left & right side of the stage



End-Fire Arrays Split Left & Right

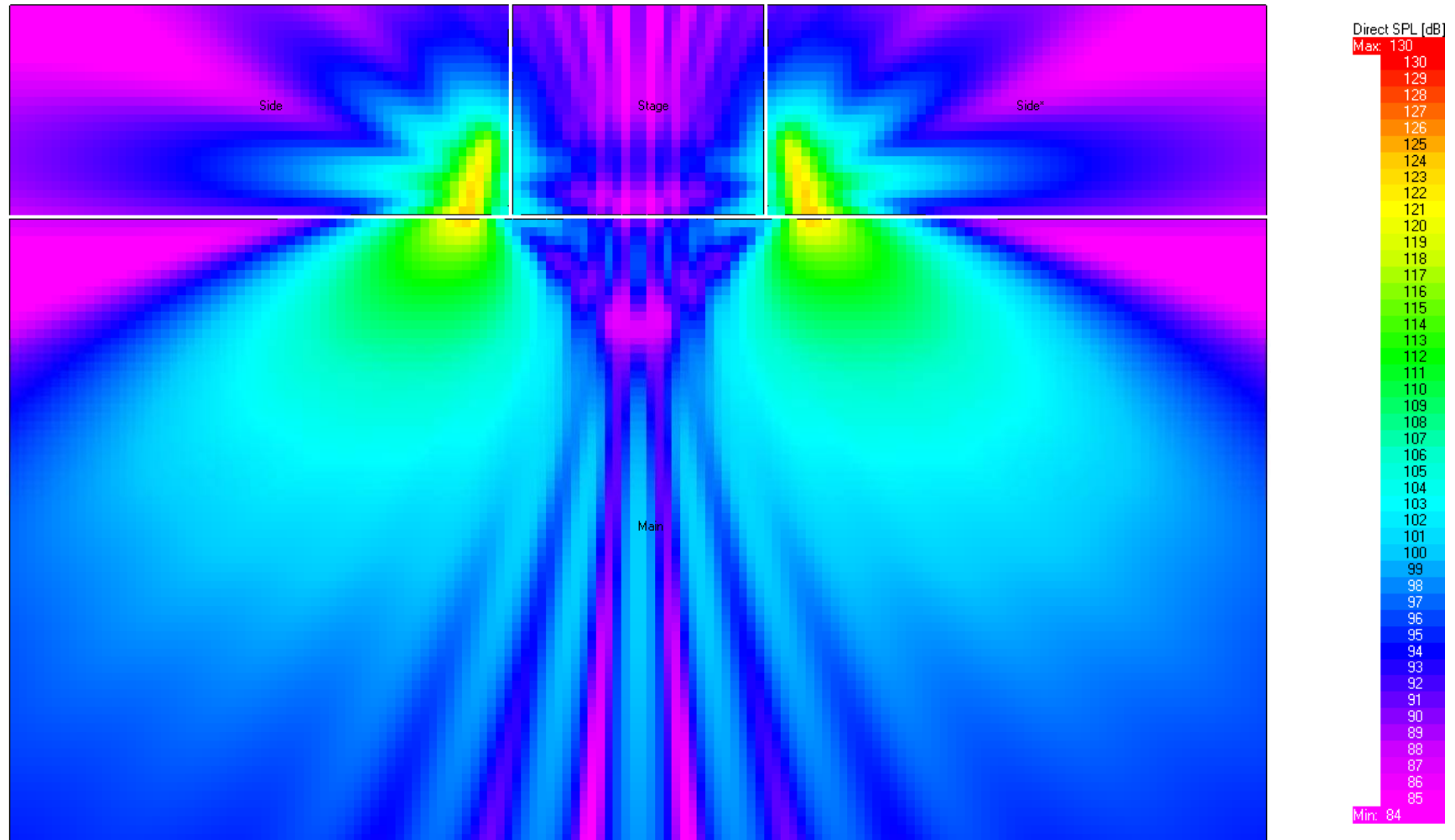


SPL Map

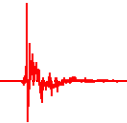


End-Fire Arrays Split Left & Right

Each array rotated 15°

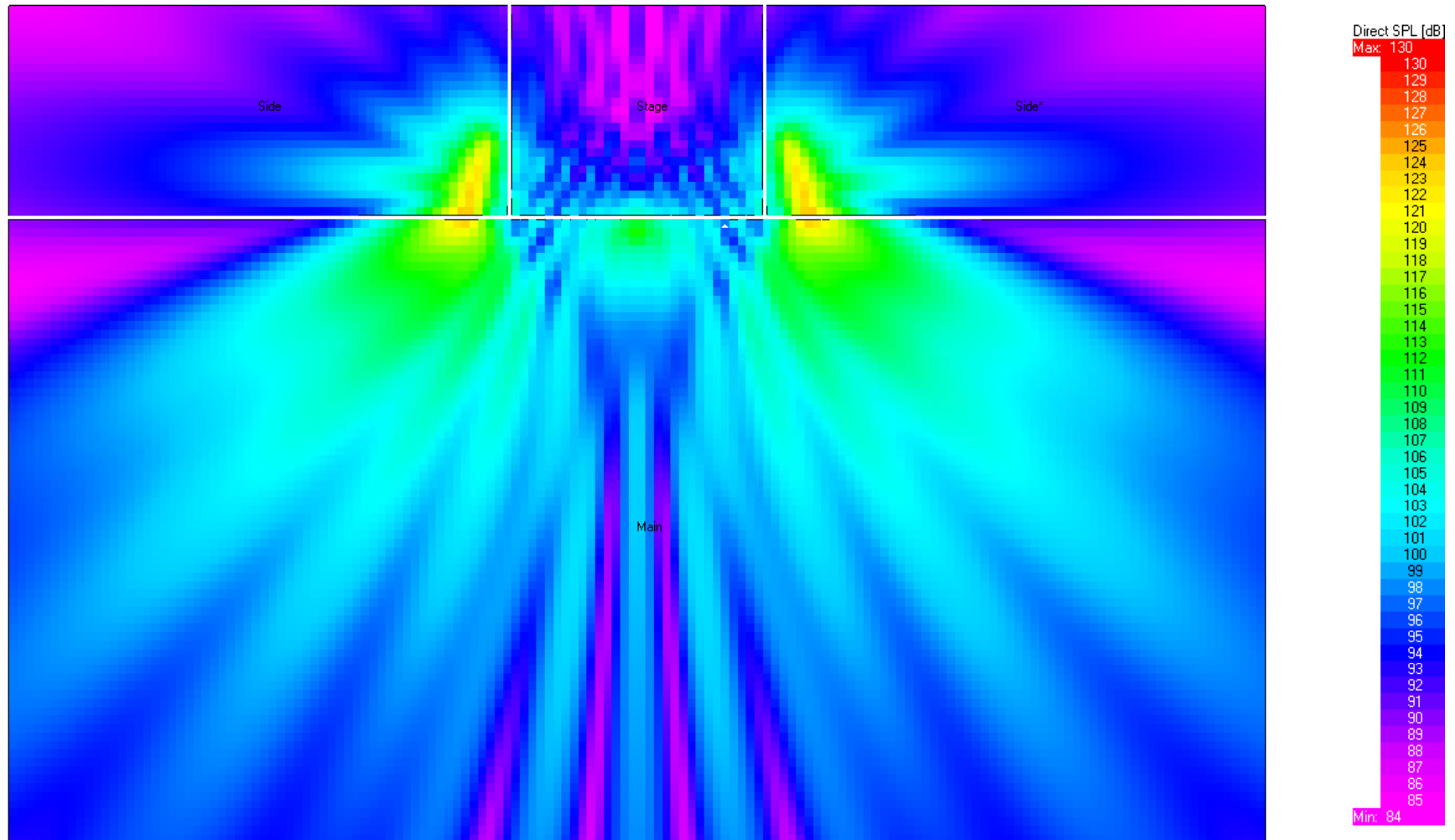


SPL Map



End-Fire Arrays Split Left & Right

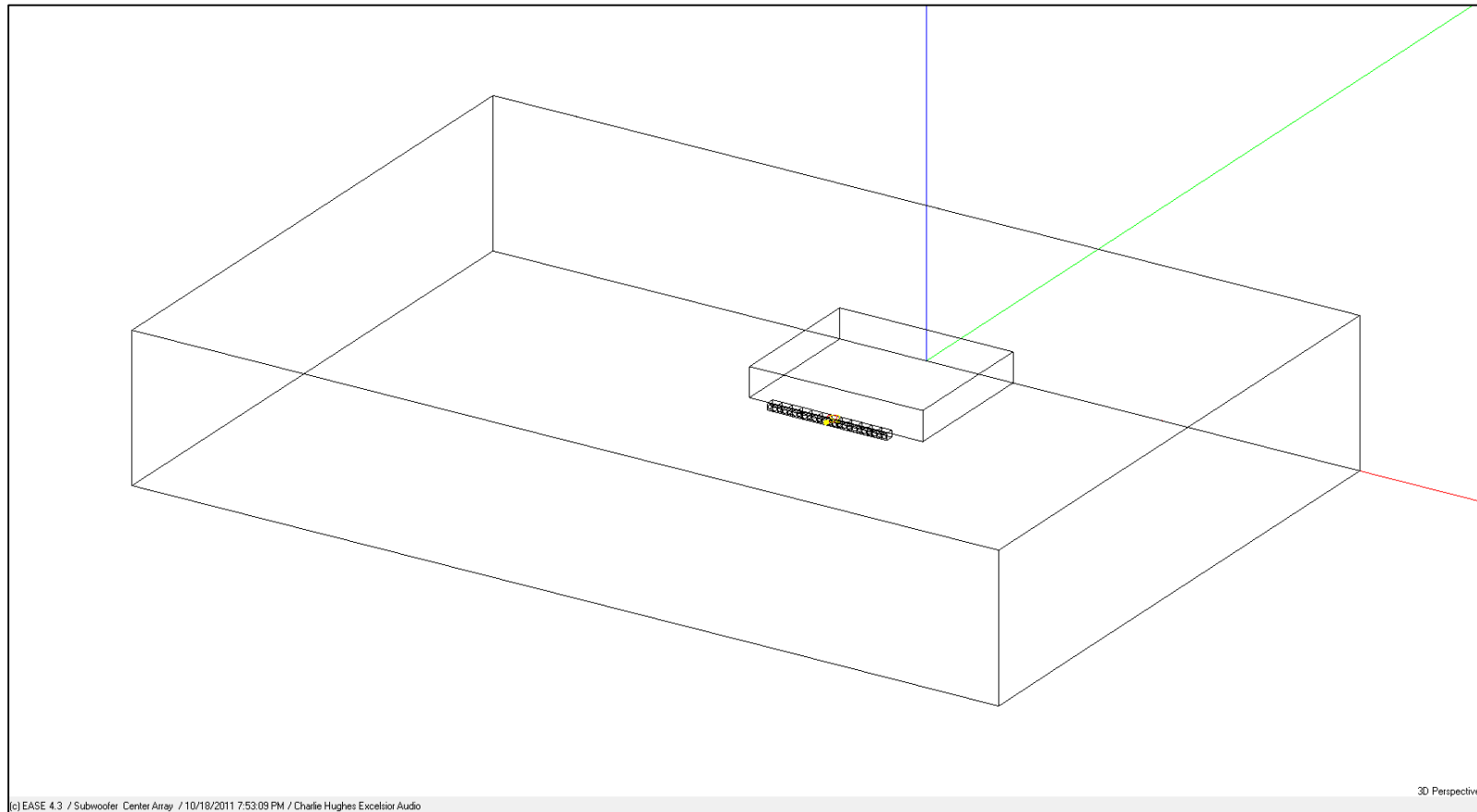
Each array rotated 15°. Center 3 box cardioid array added.



SPL Map

Center Array

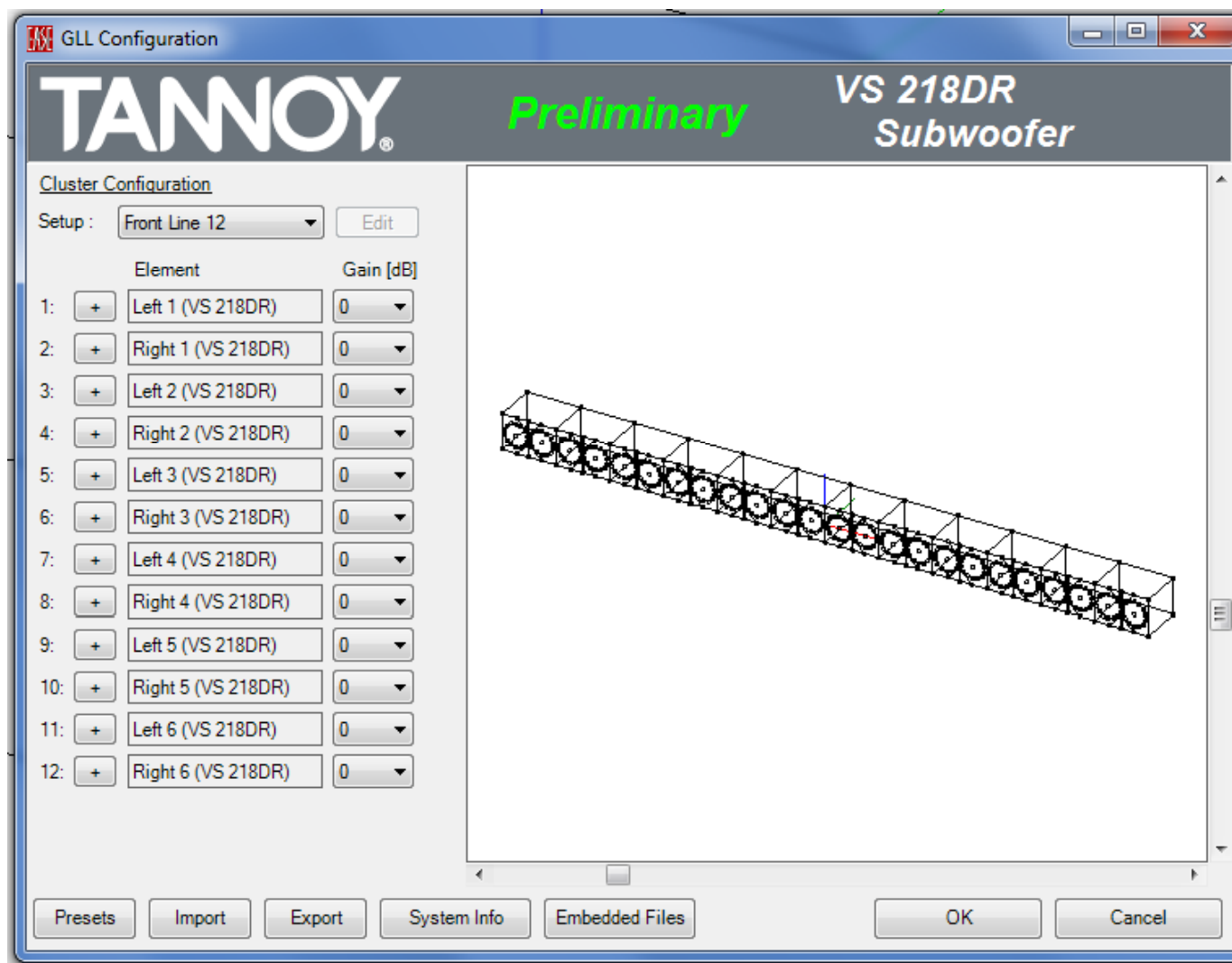
Large room (walls, floor, & ceiling are non-reflective; direct field only)
Stage approx. 60 ft (18.3 m) wide.



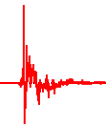
12 box straight array in center position



Center Array

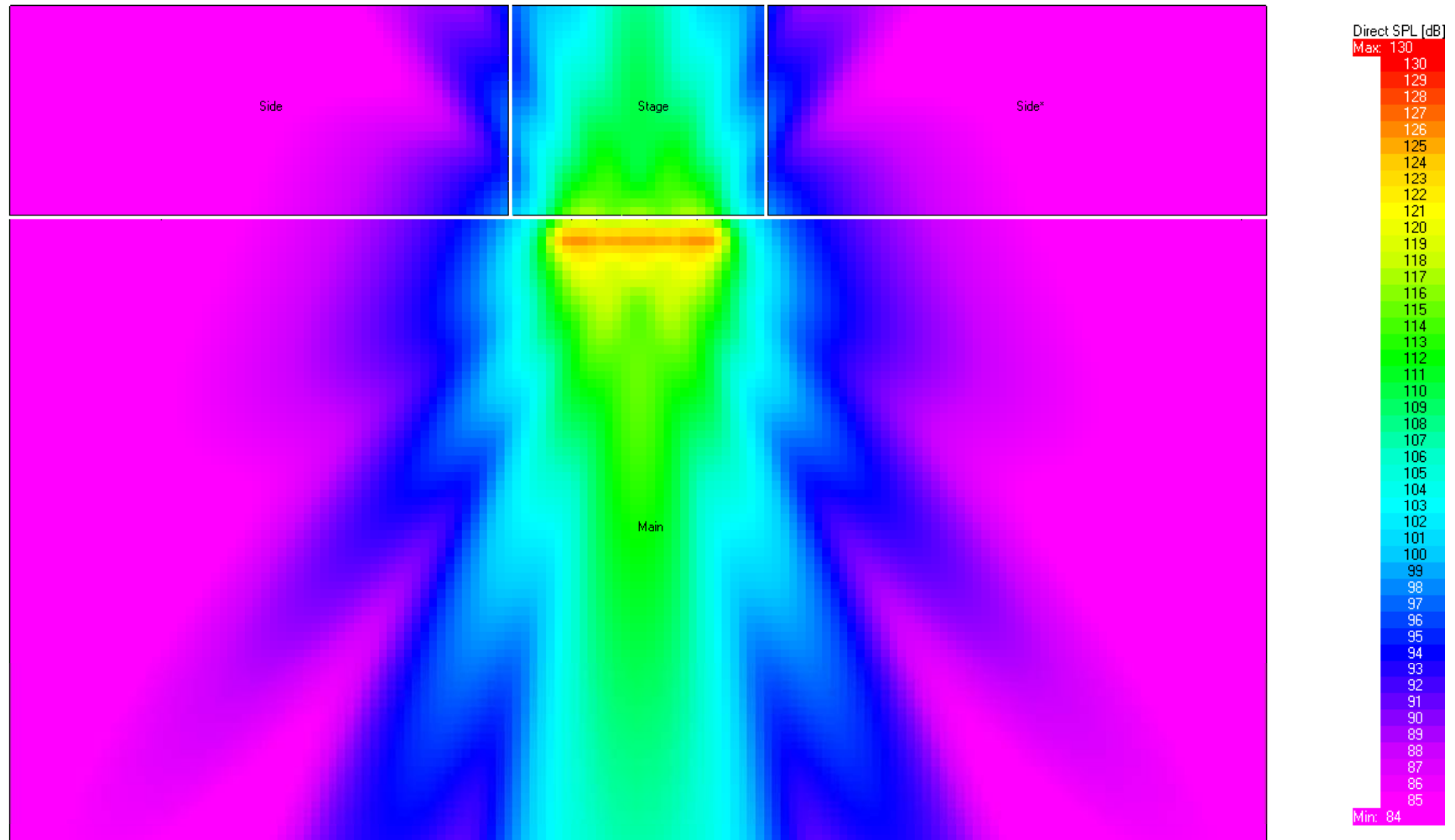


12 box straight array in center position



Center Array

Straight array (12 box) with no electronic curvature

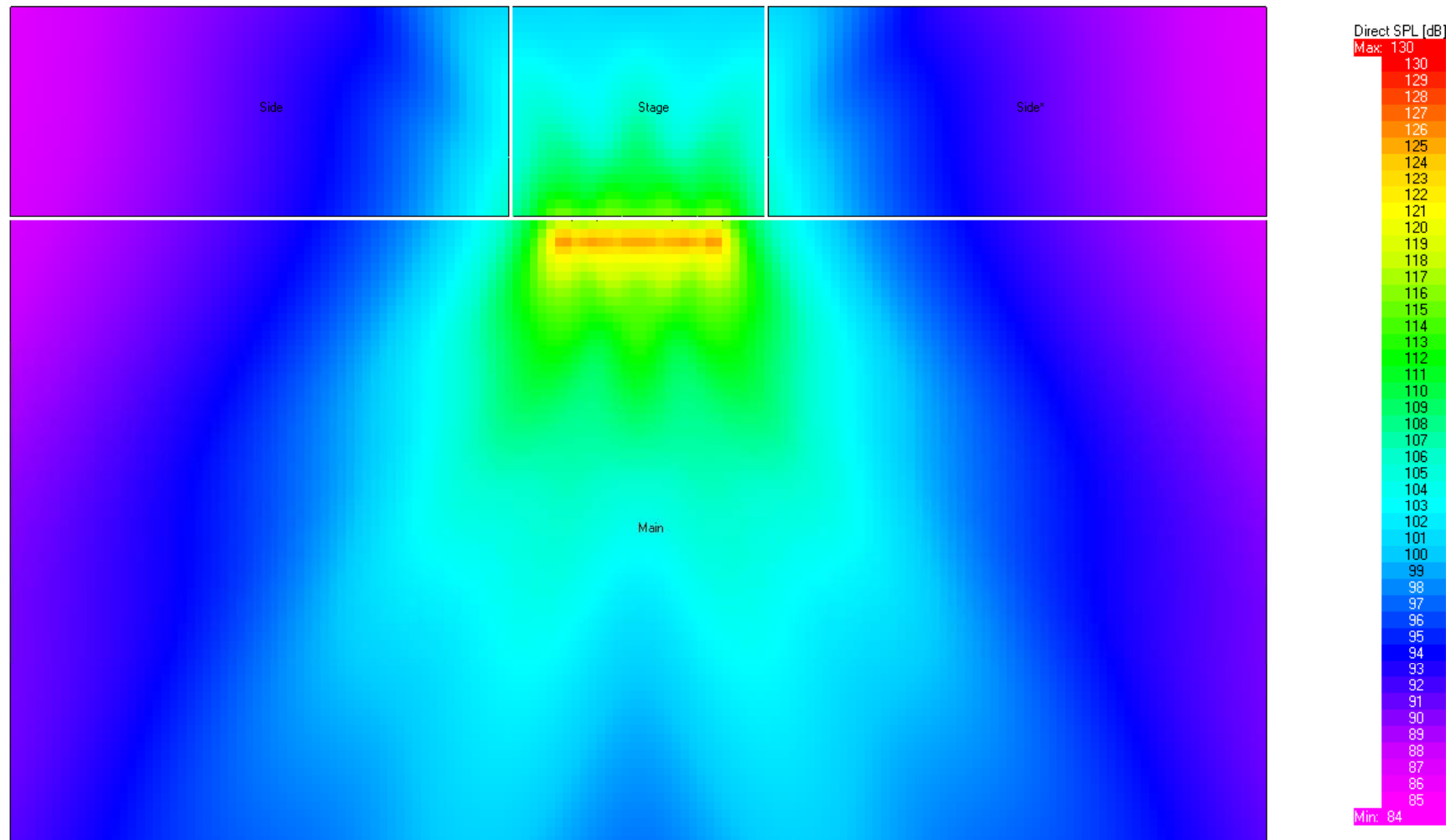


SPL Map



Center Array

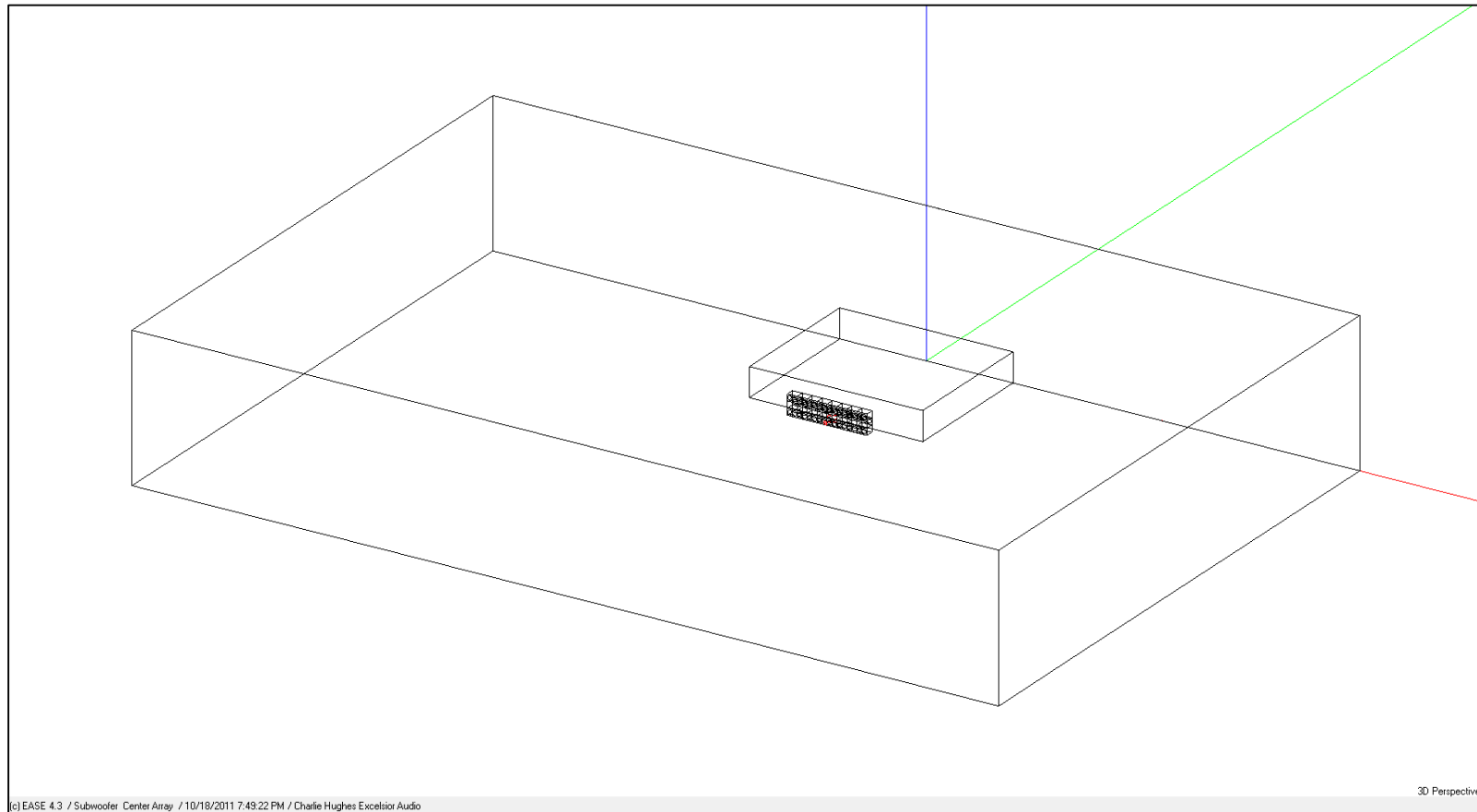
Straight array (12 box) with 90° electronic curvature



SPL Map

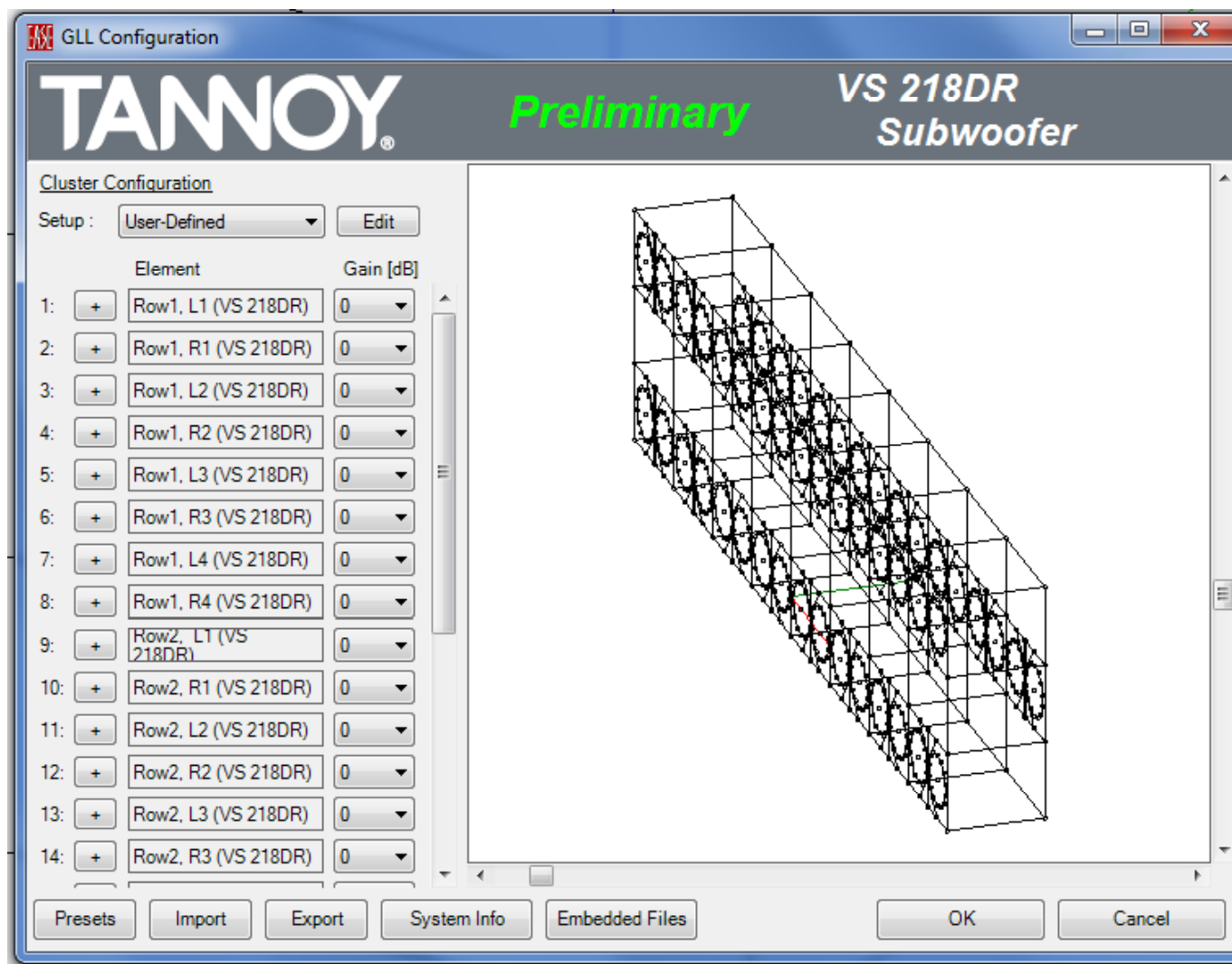
Center Cardioid Array

Large room (walls, floor, & ceiling are non-reflective; direct field only)
Stage approx. 60 ft (18.3 m) wide.



3x8 box straight array in center position

Center Cardioid Array

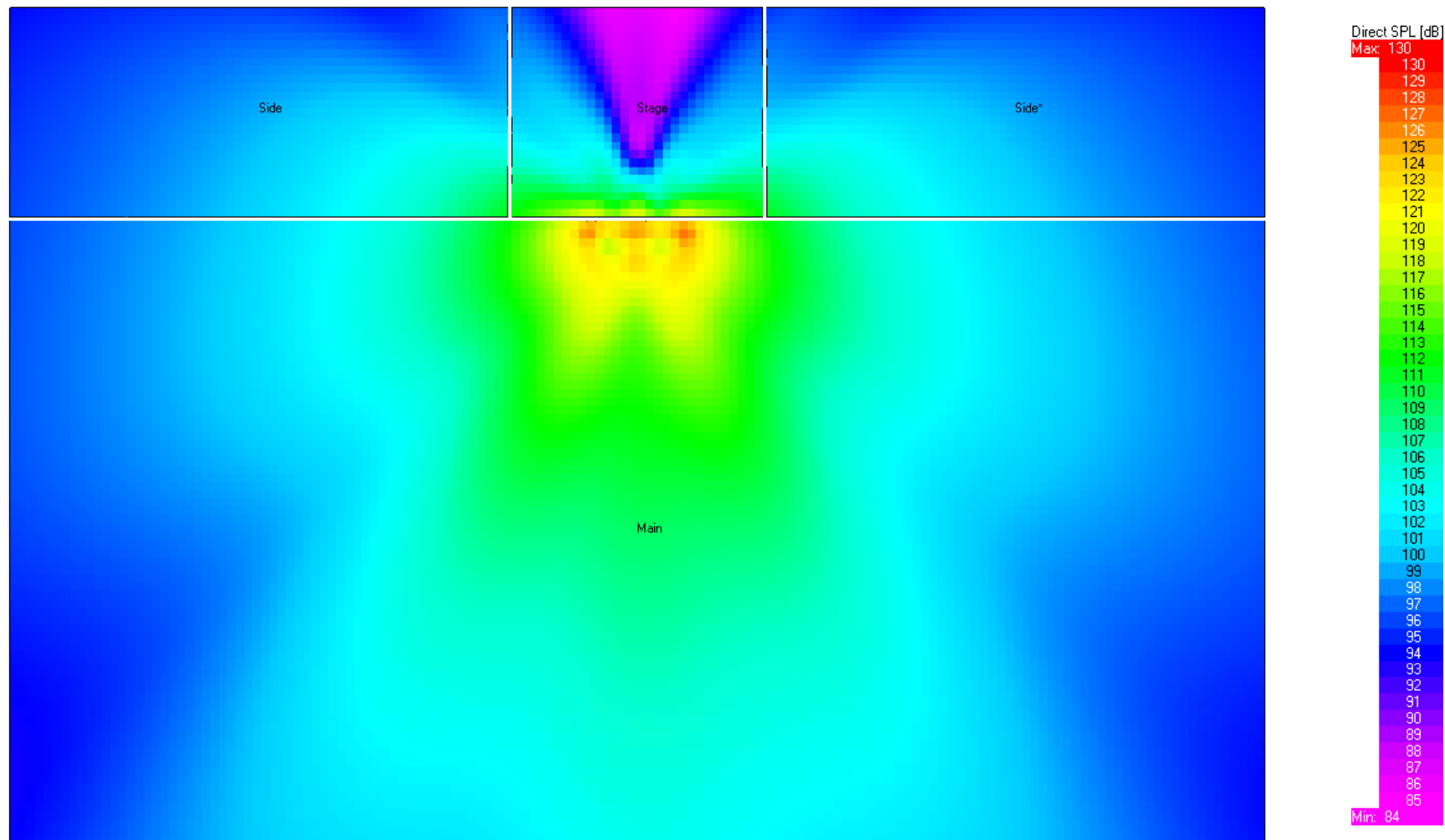


3x8 box straight array in center position

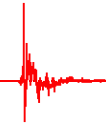


Center Array

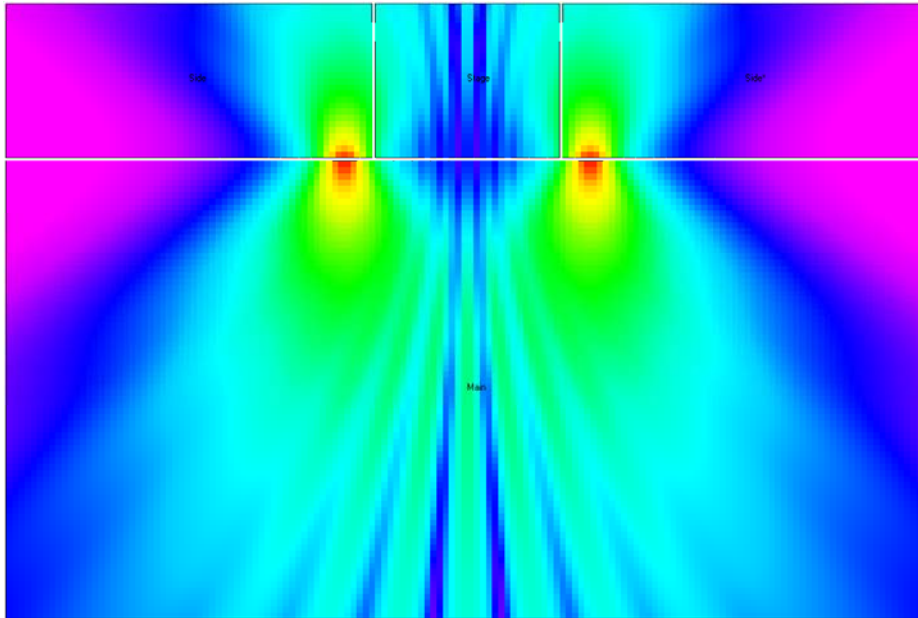
Straight array (3x 8 box stack) with 90° electronic curvature & cardioid



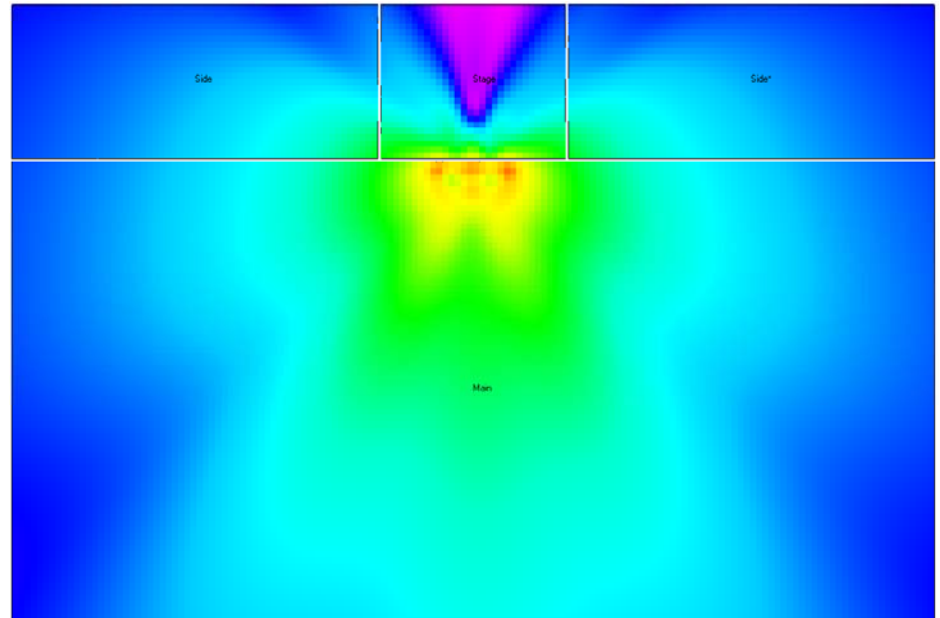
SPL Map



Comparison



Conventional split left & right



Center cardioid array eCurved 90°



Recap

Steering of the main lobe can be done electrically by applying delay to the individual subwoofer boxes.

Wave front shaping can be used to broaden the directivity, or coverage pattern, and can yield fairly constant directivity. This can also be done using delay in a DSP.

Split left & right stacks of subwoofers will always cause comb filtering & lobing.

A center array can be used to eliminate the comb filtering & lobing.

A long center cardioid array can be electronically curved to yield even coverage that is a good match to the audience area & decrease the SPL on the stage area.