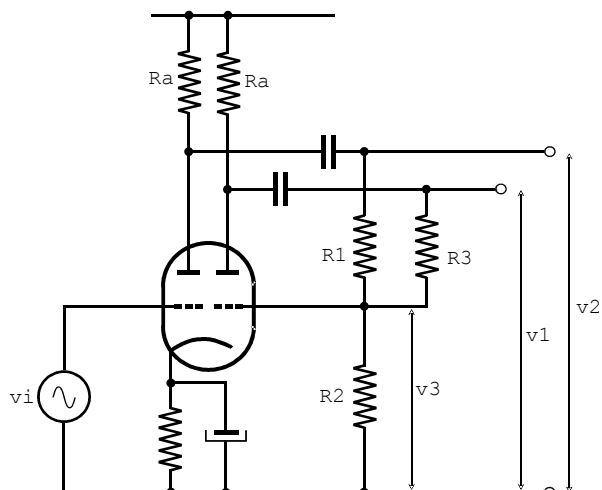


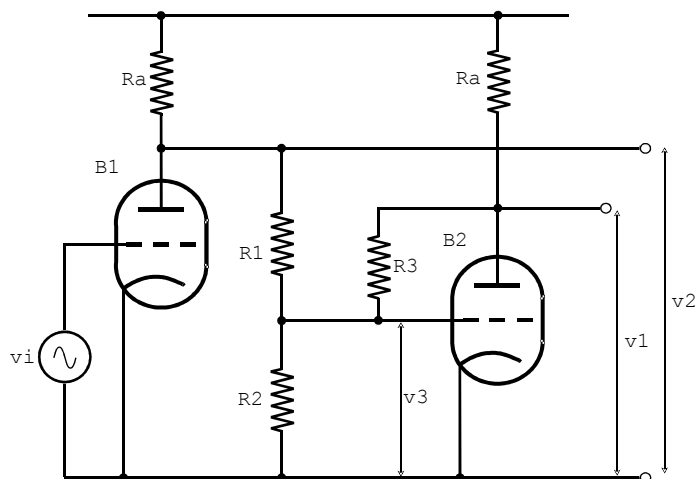
$\mu = 100;$   
 $R_i = 20\text{k}\Omega;$   
 $R_a = 80\text{k}\Omega;$   
 $R_1 = 400\text{k}\Omega;$   
 $R_3 = 20\text{k}\Omega;$   
 $v_2 = -v_1$

Calculate the value of  $R_2$ .

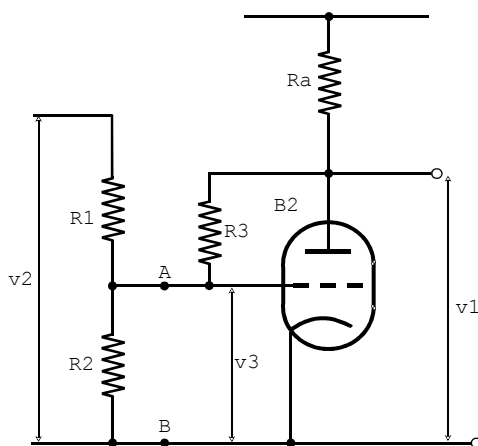


1.

For the calculation I draw an AC schematic leaving out the capacitors and using two (equal) triodes:



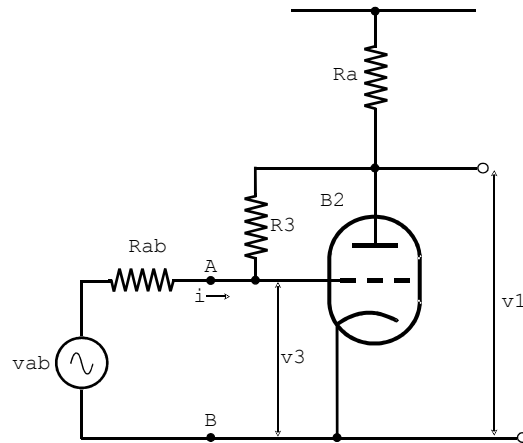
I draw again the AC diagram of the second triode from the anode of the first via the voltage divider  $R_1$ - $R_2$  to the second triode:



Using Thevenin's theorem by opening the circuit between terminals A-B and calculating the equivalent voltage  $V_{ab}$  and the equivalent impedance  $R_{ab}$ :

$$v_{ab} = \frac{R_2}{R_1 + R_2} \cdot v_2 \quad ; \quad R_{ab} = \frac{R_1 \cdot R_2}{R_1 + R_2}$$

We can redraw the circuit:



In the circuit above:

$$i = \frac{v_{ab} - v_3}{R_{ab} + R_3} \quad i = \frac{v_3 - v_1}{R_3}$$

And:

$$\frac{v_{ab} - v_3}{R_{ab} + R_3} = \frac{v_3 - v_1}{R_3}$$

$$\frac{v_{ab}}{R_{ab}} - \frac{v_3}{R_{ab}} = \frac{v_3}{R_3} - \frac{v_1}{R_3}$$

$$\frac{v_{ab}}{R_{ab}} = \frac{v_3}{R_{ab}} + \frac{v_3}{R_3} - \frac{v_1}{R_3}$$

$$\frac{v_{ab}}{R_{ab}} = v_3 \left( \frac{1}{R_{ab}} + \frac{1}{R_3} \right) - \frac{v_1}{R_3}$$

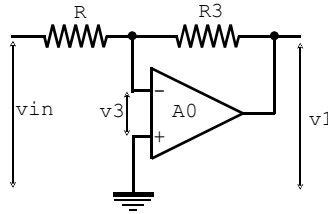
We also know that:

$$\frac{v_{ab}}{R_{ab}} = \frac{R_2}{R_1 + R_2} \cdot \frac{R_1 + R_2}{R_1 \cdot R_2} \cdot v_2$$

$$\frac{v_{ab}}{R_{ab}} = \frac{v_2}{R_1}$$

$$\frac{v_2}{R_1} = v_3 \left( \frac{1}{R_{ab}} + \frac{1}{R_3} \right) - \frac{v_1}{R_3} \quad (1)$$

To calculate the open loop gain remember opamp theory:



In op-amps the open loop gain is very high so the value of  $v_3$  is always neglected when calculating the transfer function, but with the triode this gain can be maximum  $\mu$  theoretically.

$$v_3 = \frac{v_1}{A_0} \quad \text{where } A_0 \text{ is the open loop gain of the triode.}$$

Substituting this in (1) gives:

$$\frac{v_2}{R_1} = \frac{v_1}{A_0} \left( \frac{1}{R_{ab}} + \frac{1}{R_3} \right) - \frac{v_1}{R_3} \quad (1a)$$

$$v_2 = \frac{v_1}{A_0} \left( \frac{R_1}{R_{ab}} + \frac{R_1}{R_3} \right) - \frac{R_1}{R_3} \cdot v_1$$

$$v_2 = v_1 \left\{ \frac{1}{A_0} \left( \frac{R_1}{R_{ab}} + \frac{R_1}{R_3} \right) - \frac{R_1}{R_3} \right\}$$

$$\frac{v_2}{v_1} = \frac{1}{A_0} \left( \frac{R_1}{R_{ab}} + \frac{R_1}{R_3} \right) - \frac{R_1}{R_3} \quad (1b)$$

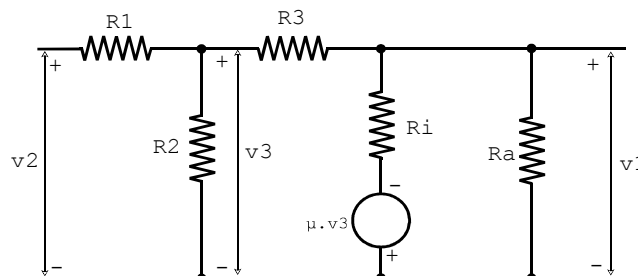
And because:

$$R_{ab} = \frac{R_1 \cdot R_2}{R_1 + R_2}$$

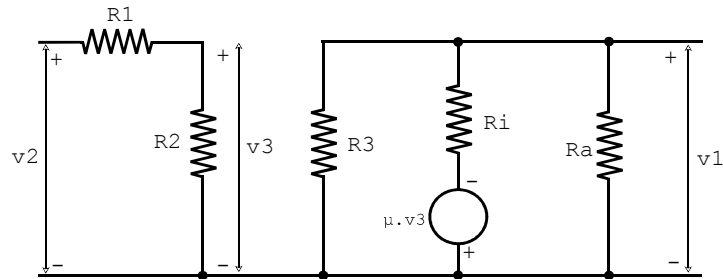
Substituting this in (1b):

$$\frac{v_2}{v_1} = \frac{1}{A_0} \left( 1 + \frac{R_1}{R_2} + \frac{R_1}{R_3} \right) - \frac{R_1}{R_3} \quad (2)$$

Now we have to calculate  $A_0$  drawing the equivalent 'pi' circuit:



And disconnect the feedback resistor R3 and connect it to the common:



And calculate the open loop gain:

$$v1 = \frac{Rv}{Ri + Rv} \cdot \mu \cdot v3$$

Where Rv is the equivalent of Ra//R3

$$\frac{v1}{v3} = A0 = \frac{\mu \cdot Rv}{Ri + Rv}$$

Substituting the values:

$$A0 = \frac{100 \cdot 16}{20 + 16} = 44,4$$

Writing eq. (2) again and substituting the values:

$$\frac{v2}{v1} = \frac{1}{A0} \left( 1 + \frac{R1}{R2} + \frac{R1}{R3} \right) - \frac{R1}{R3} \quad (2)$$

$$\frac{v2}{v1} = -1 ; R1 = 400 \text{ k}\Omega ; R3 = 20 \text{ k}\Omega ; A0 = 44,44$$

$$-1 = \frac{1}{44,44} \left( 1 + \frac{400}{R2} + \frac{400}{20} \right) - \frac{400}{20}$$

$$-1 = 0,0225 + \frac{9}{R2} + 0,45 - 20$$

$$-1 = \frac{9}{R2} - 19,53$$

$$18,53 \cdot R2 = 9$$

$$R2 = \frac{9}{18,53} = 0,486 \text{ k}\Omega = 486 \Omega$$